

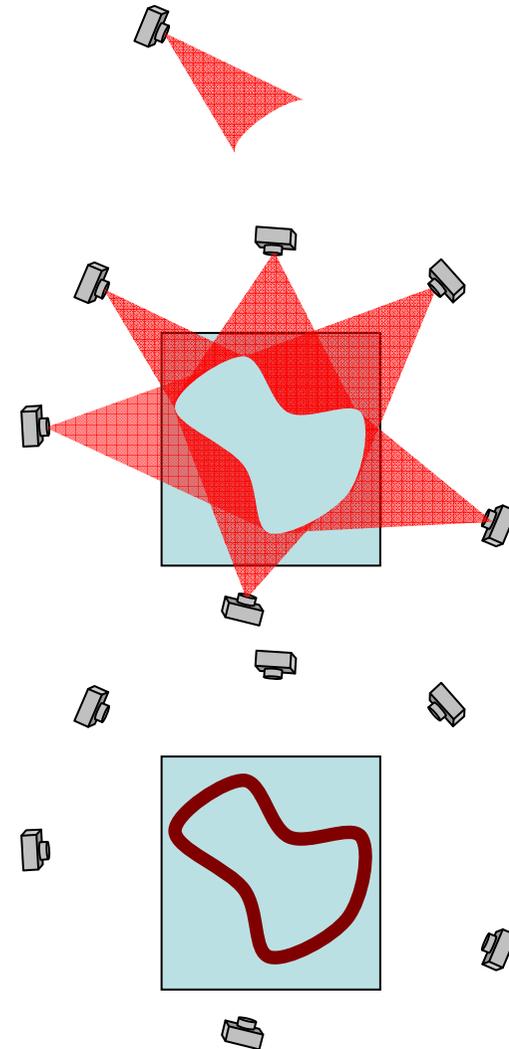
# Occlusion-robust photo-consistency

**George Vogiatzis**

([g.vogiatzis@aston.ac.uk](mailto:g.vogiatzis@aston.ac.uk))

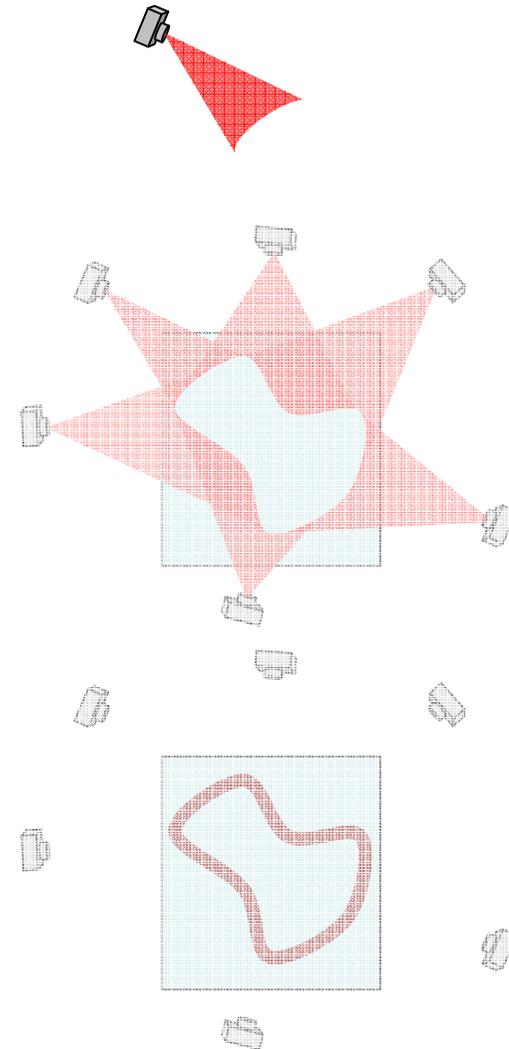
# Occlusion-robust photo-consistency

1. Compute depth-maps from each view using neighbouring views
2. Merge depth-maps into single volume
3. Extract 3d surface from this volume



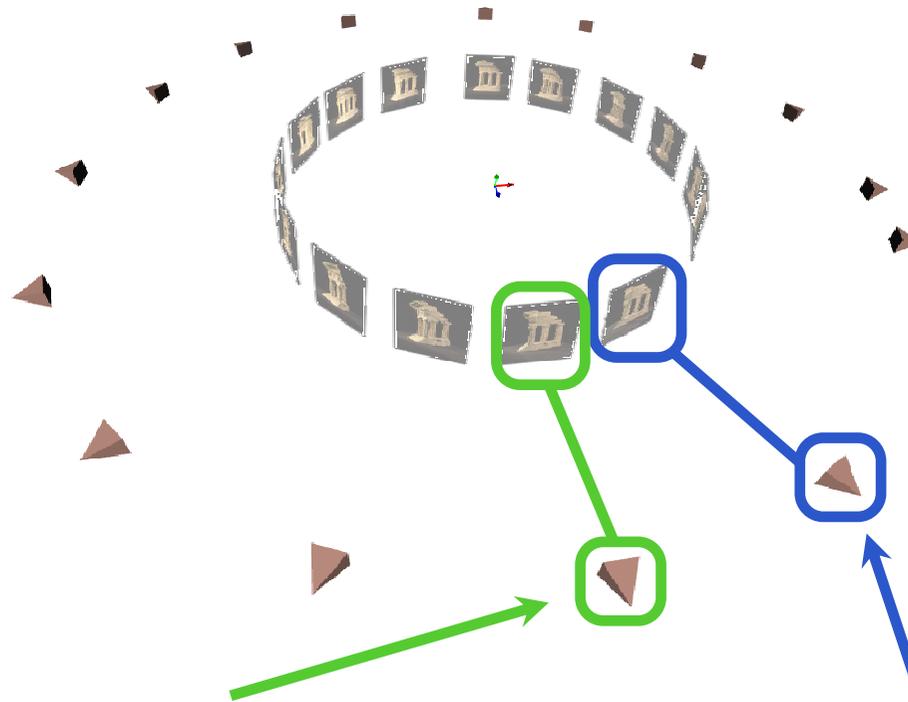
# Occlusion-robust photo-consistency

1. Compute depth-maps from each view using neighbouring views
2. Merge depth-maps into single volume
3. Extract 3d surface from this volume



# 1. Compute depth-maps

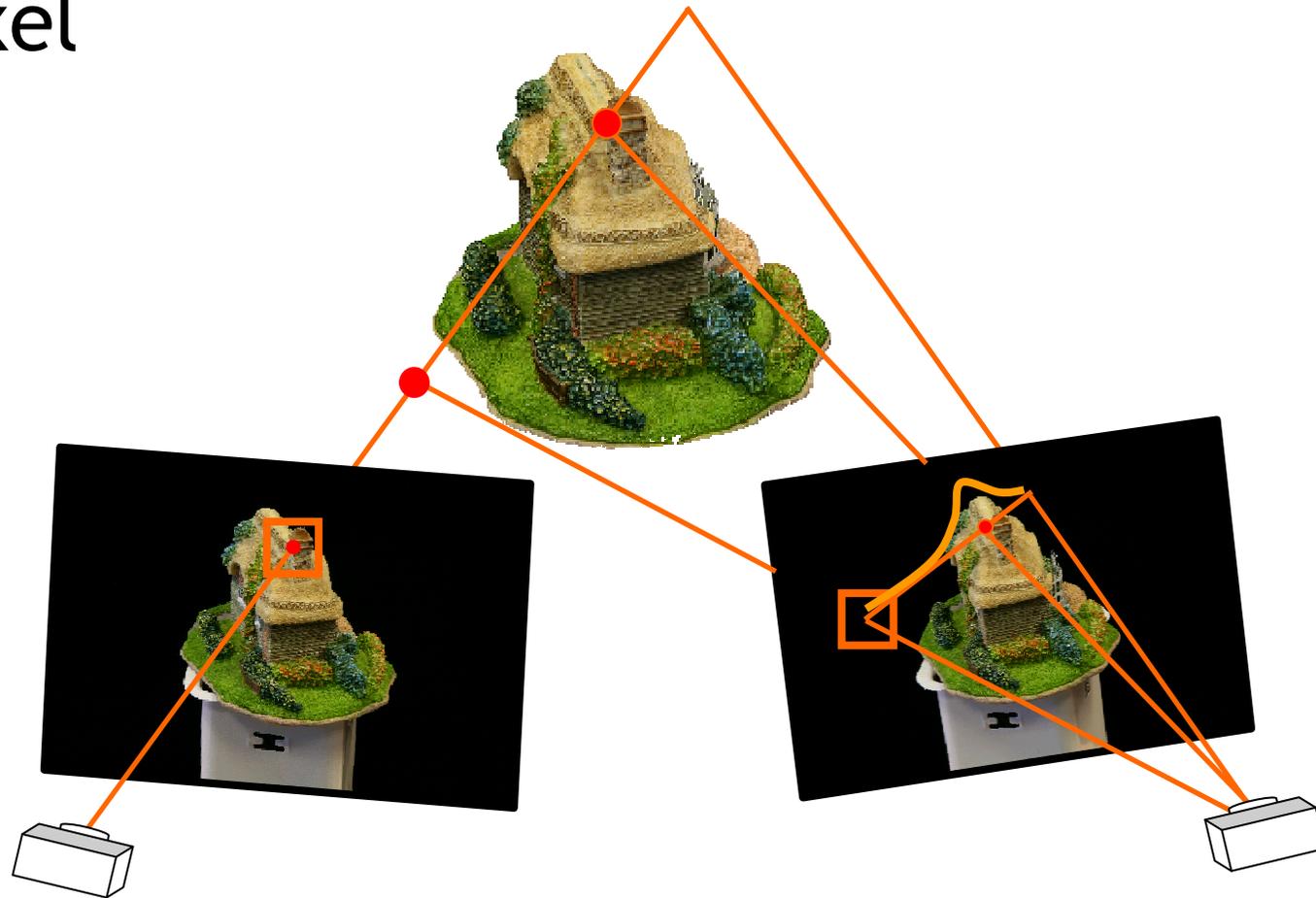
- Occlusion effects are small between neighbouring views



Select a **reference image** and a **neighbouring image**

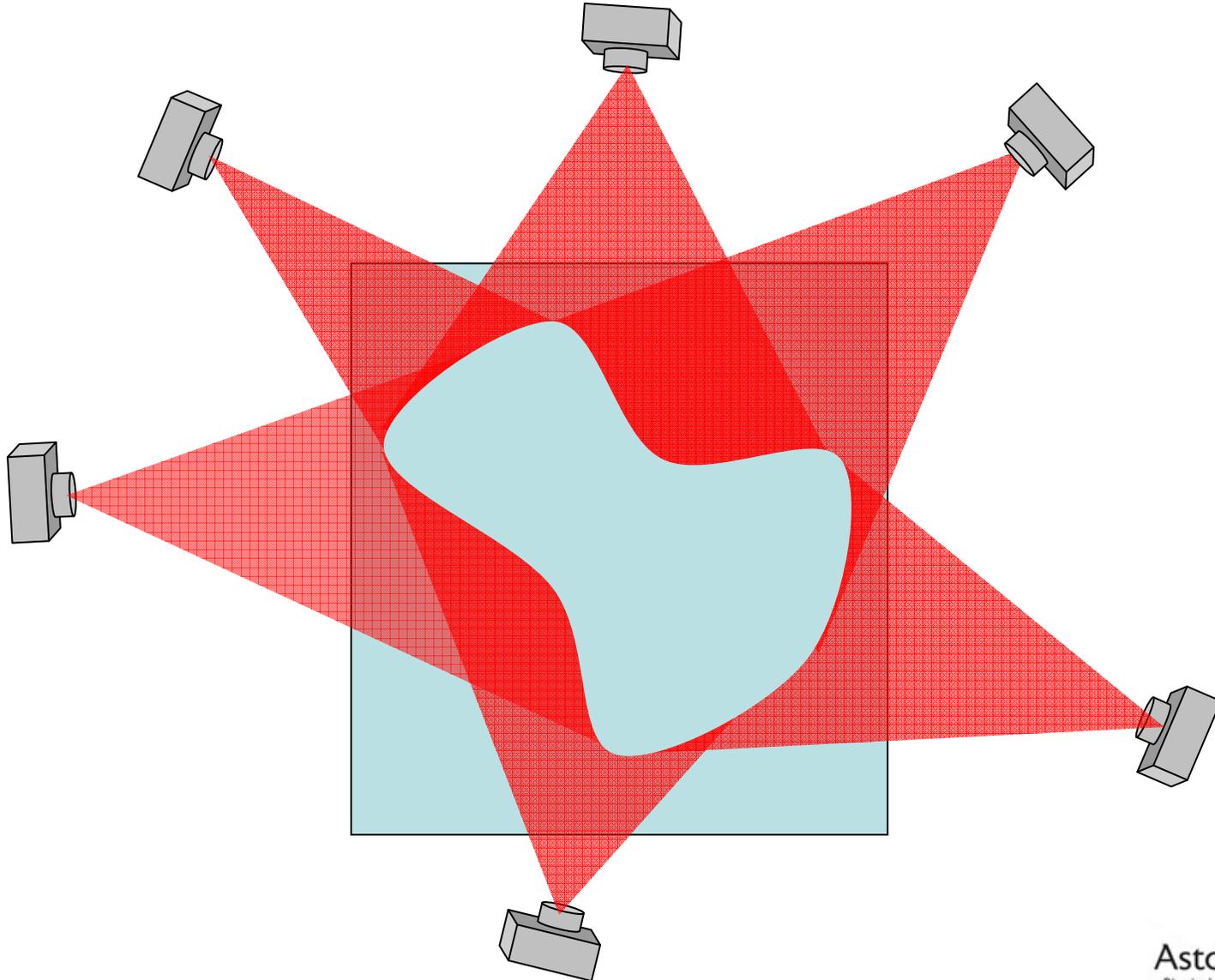
# 1. Compute depth-maps

- Use matching score to find best depth at pixel



## 2. Merge depth-maps

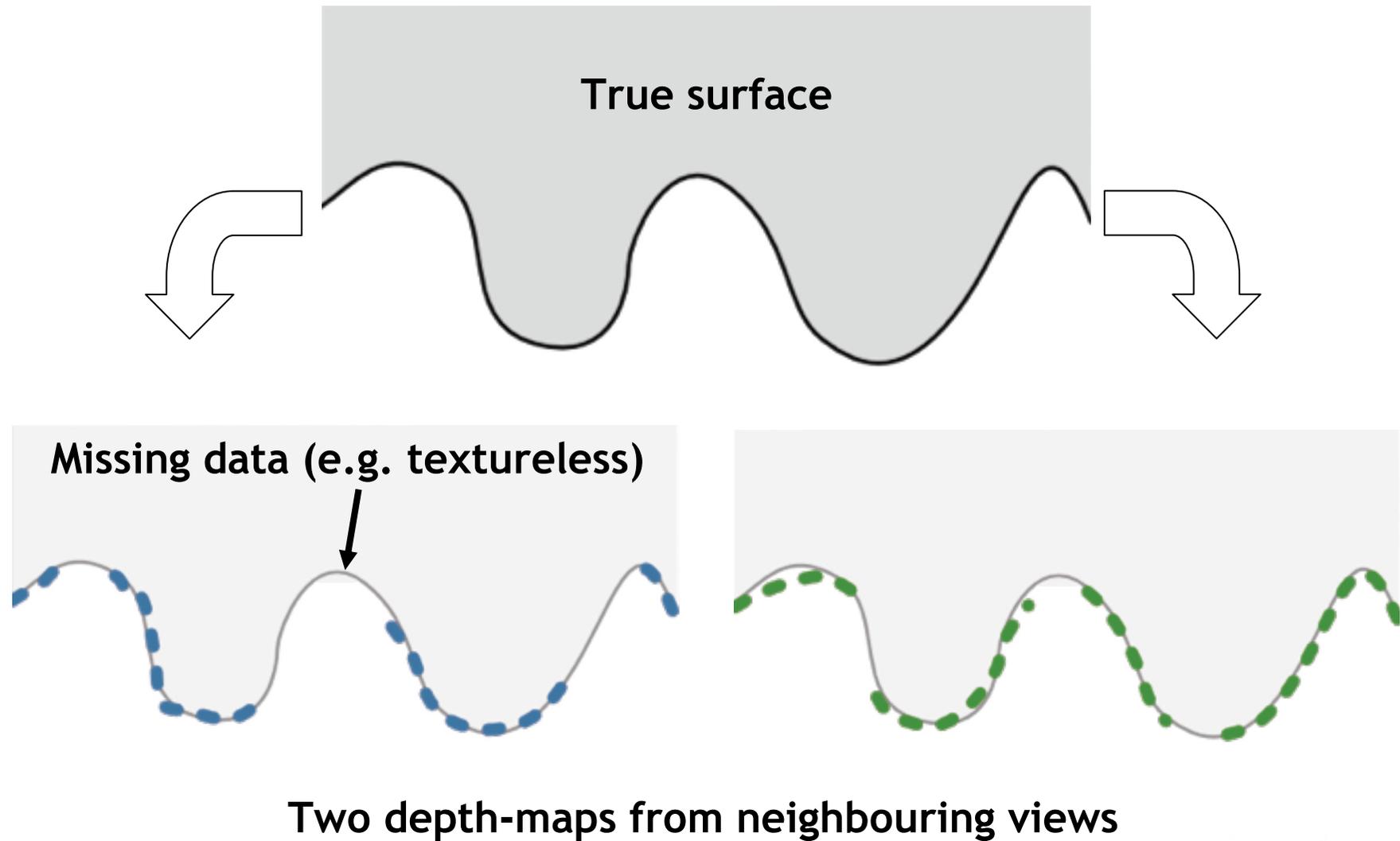
- Use efficient volumetric data-structure



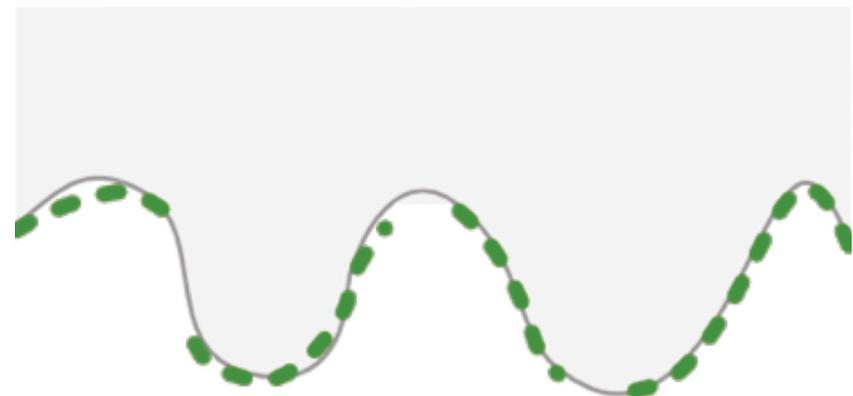
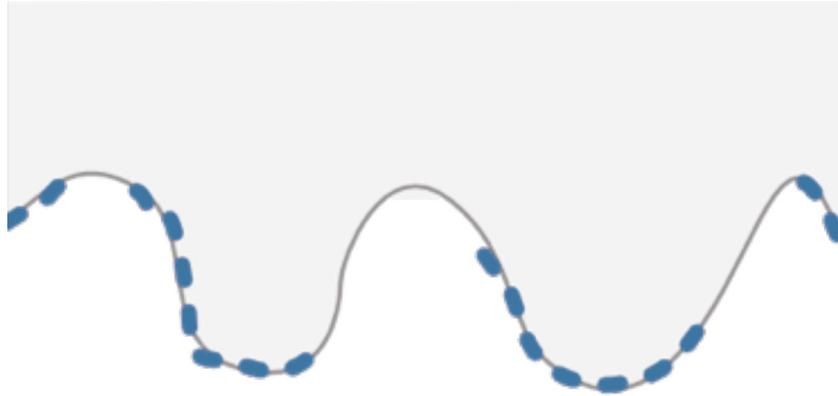
# Depth-map computation

- Why not use the best binocular stereo algorithm?
- Makes use of spatial regularisation to cope with e.g. textureless regions
- Assumes only local image data is available
- Regularises too early

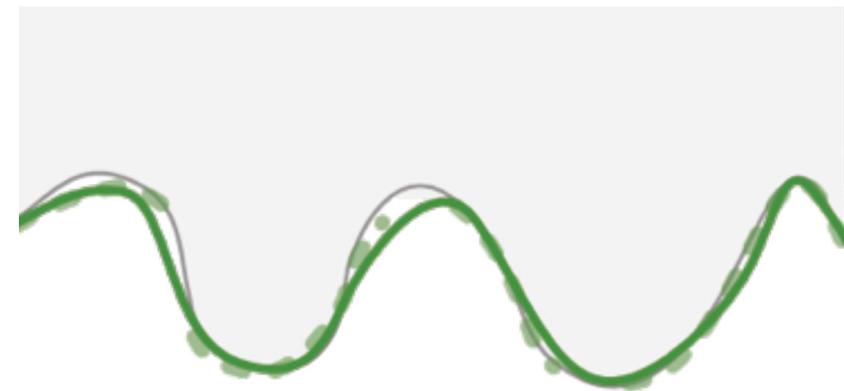
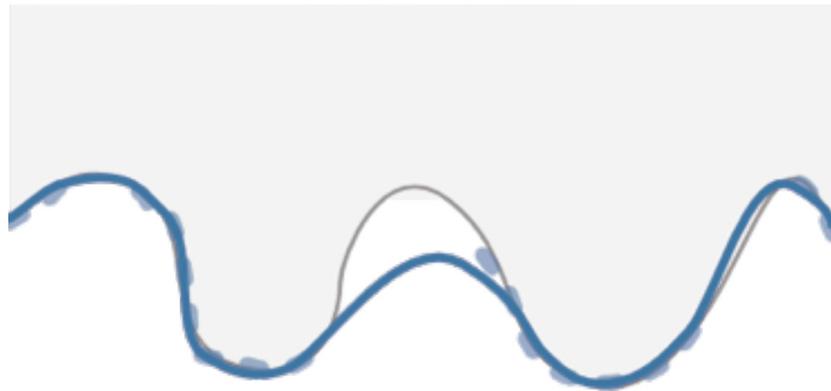
# Early regularisation



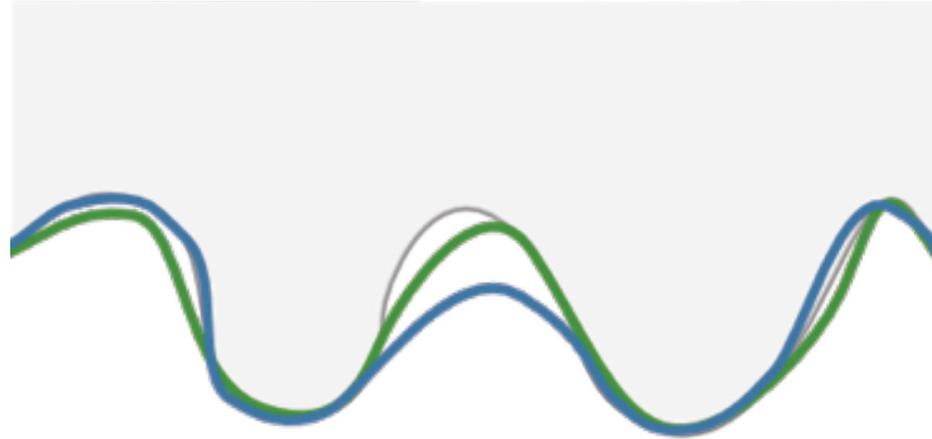
# Early regularisation



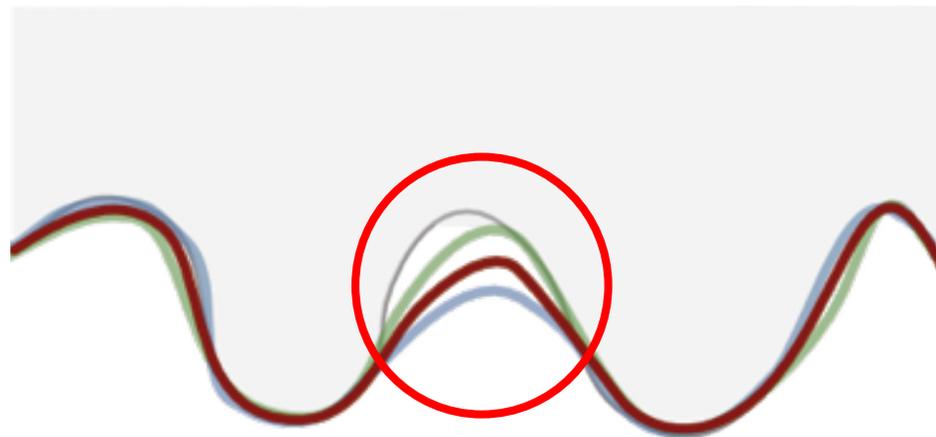
Independent regularisation for each depth-map



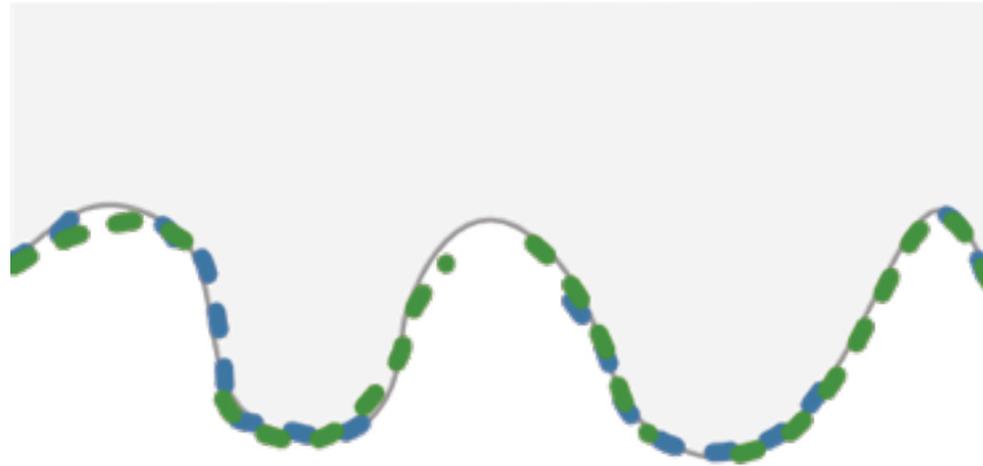
# Early regularisation



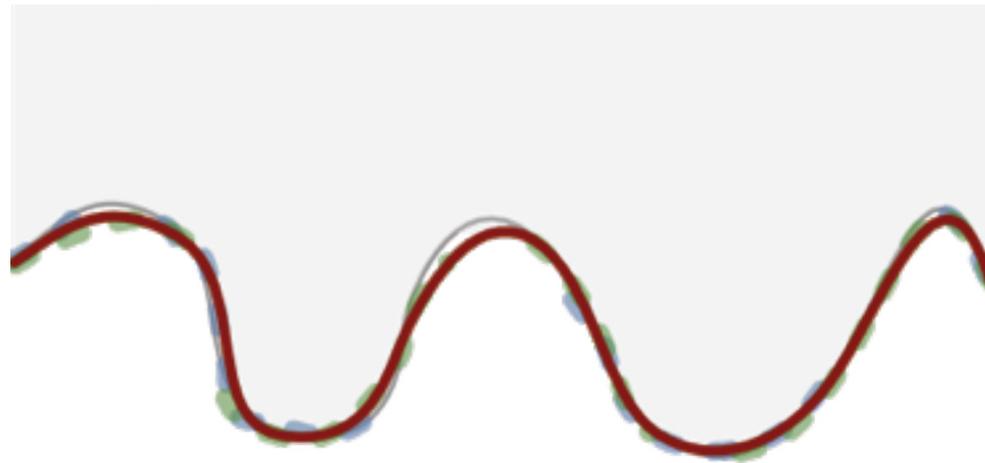
Combine the two estimates



# Early regularisation

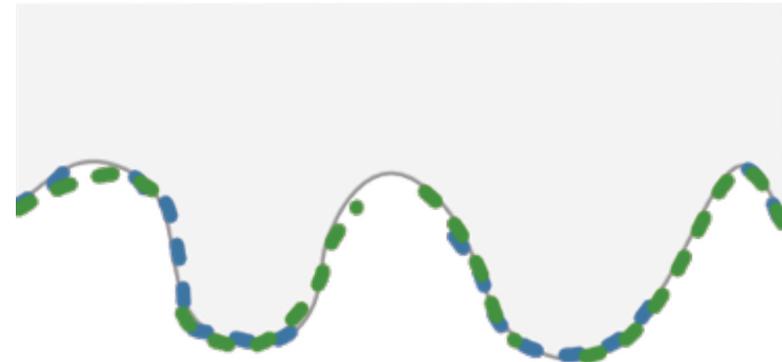
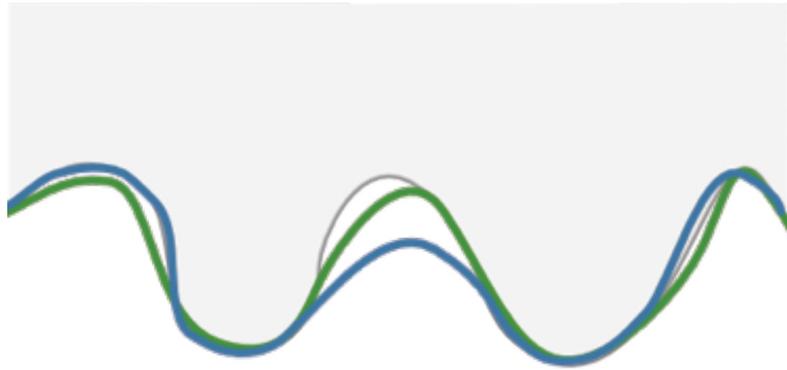


Combine the depth-maps and THEN regularise

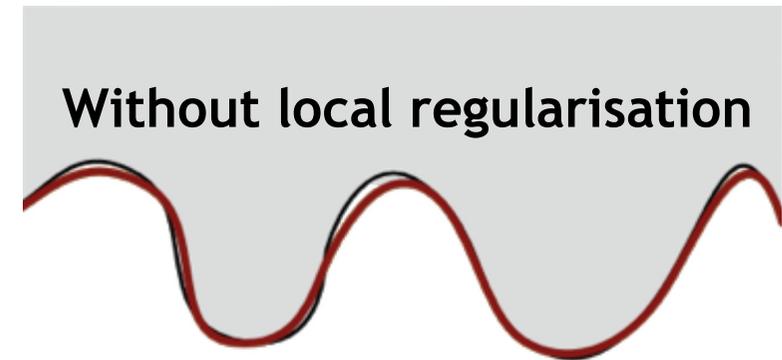
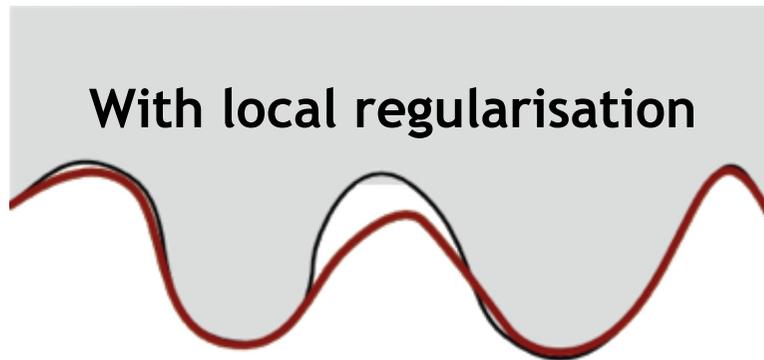


# Early regularisation

Before combining



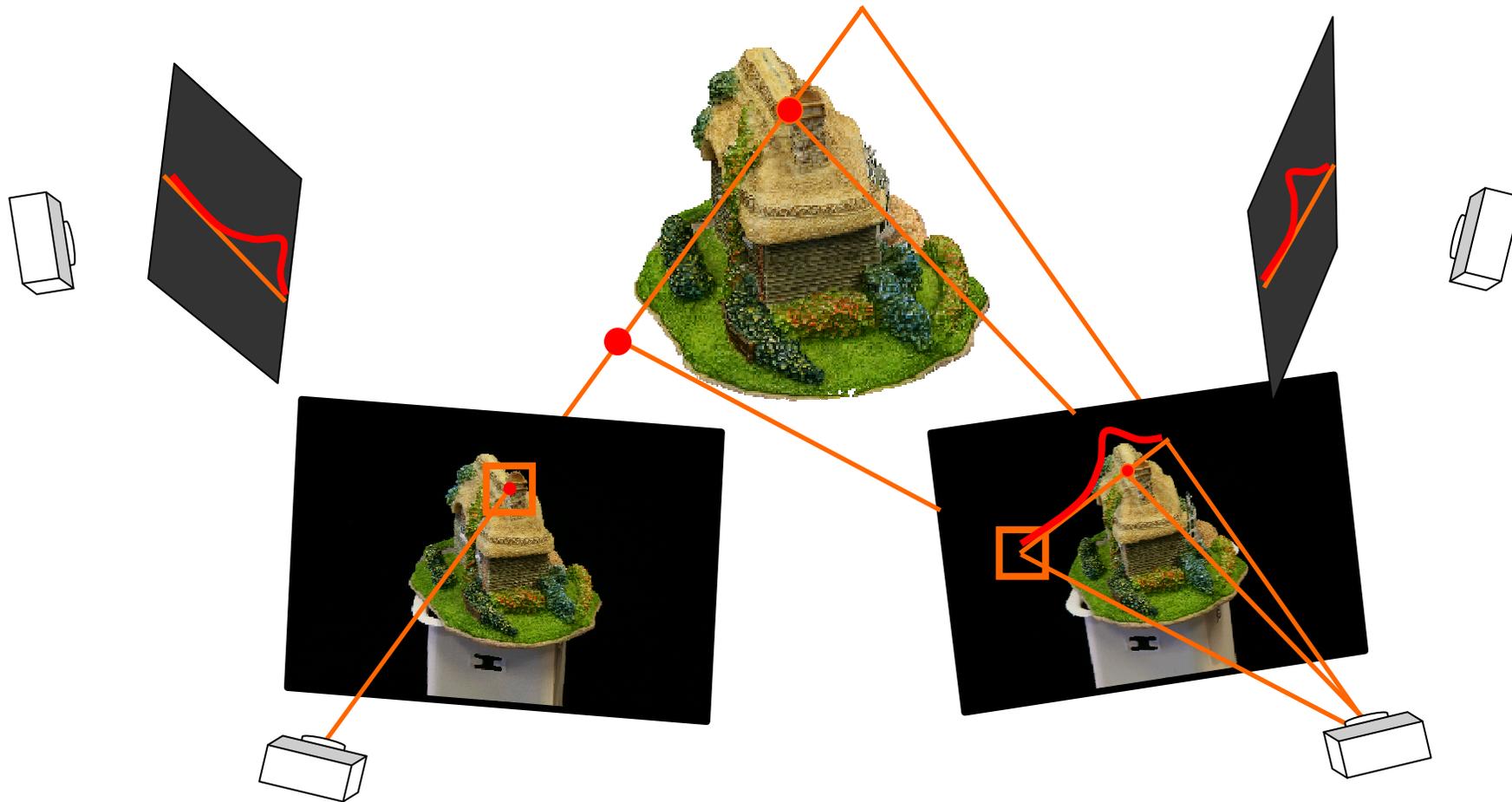
Final result



# Depth-map computation

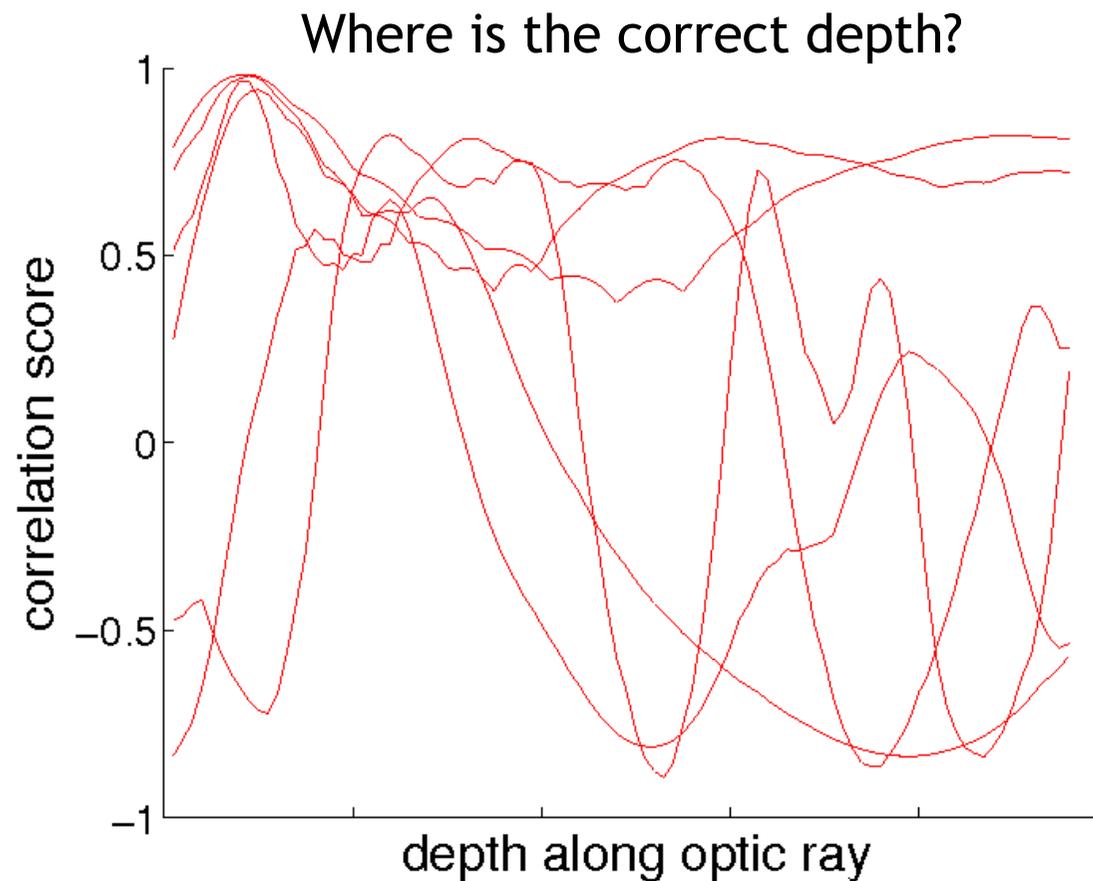
- Compute completely **unregularised** depth-maps independently for each viewpoint
- Only regularise at final stage

# Find independent depth of each pixel

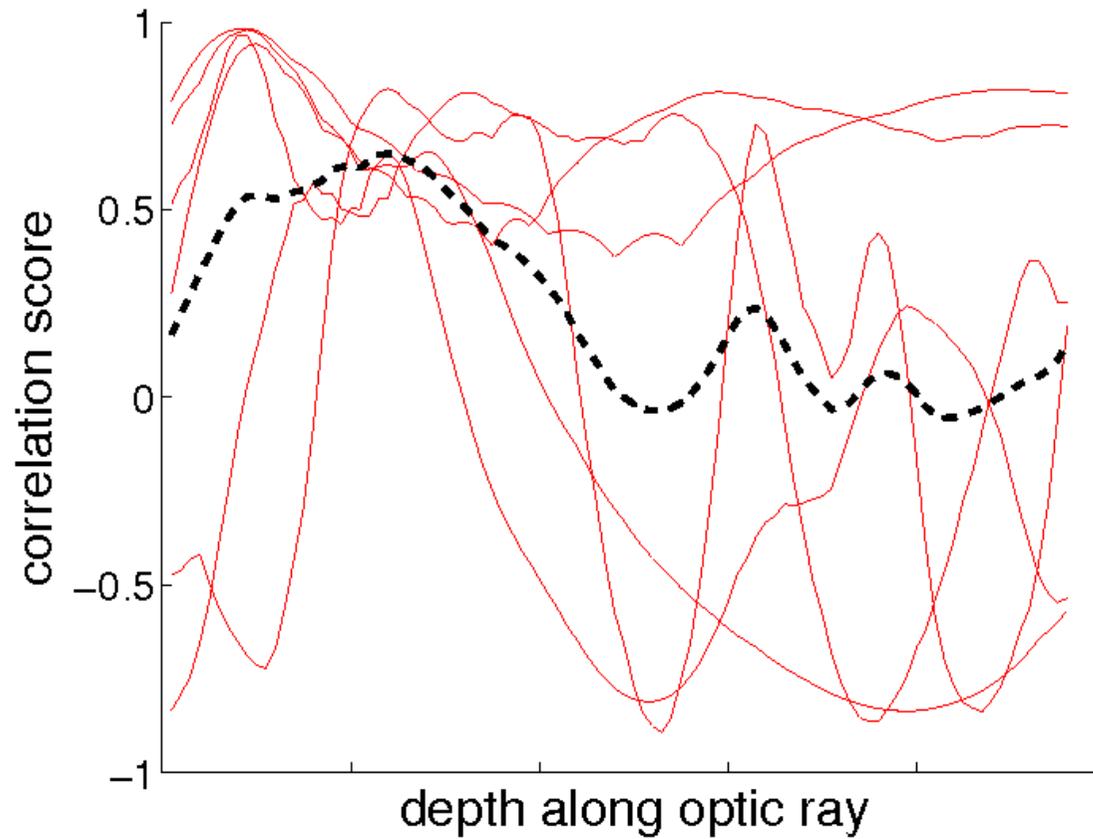


# Combining Matching scores

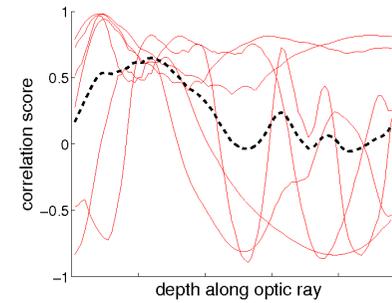
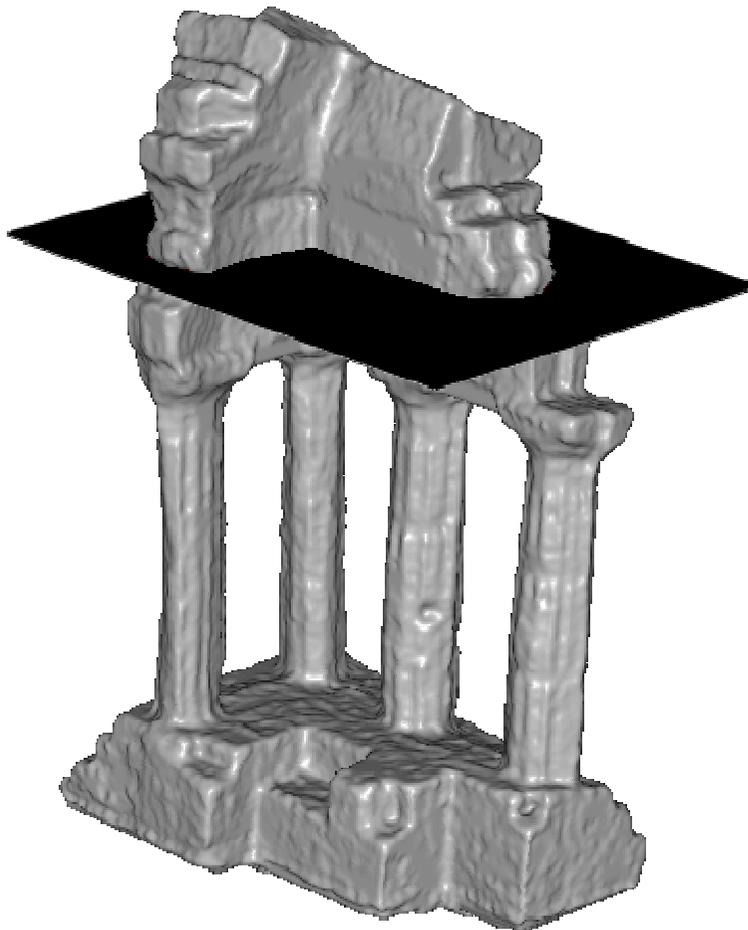
- Compute one correlation curve per image



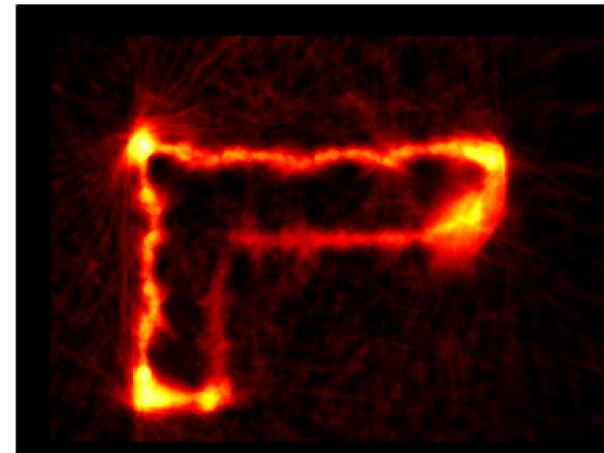
# Simple averaging



# Averaged NCC



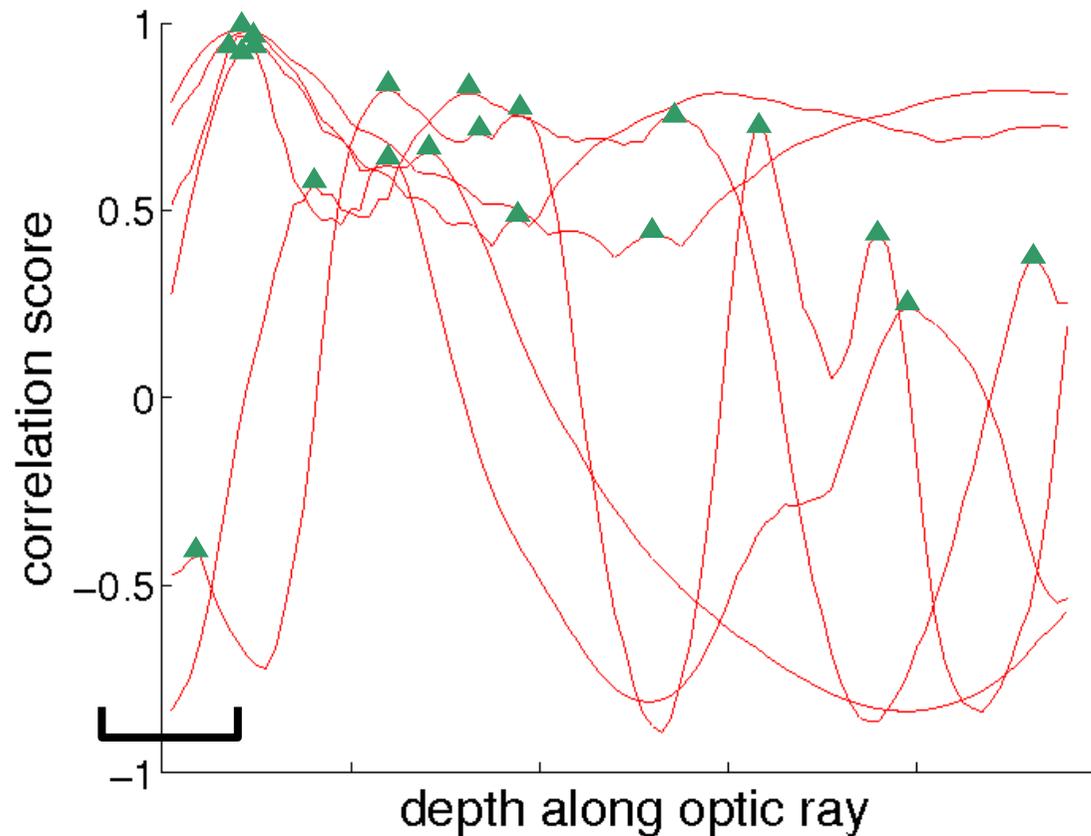
In 3d



# Peaks of matching score

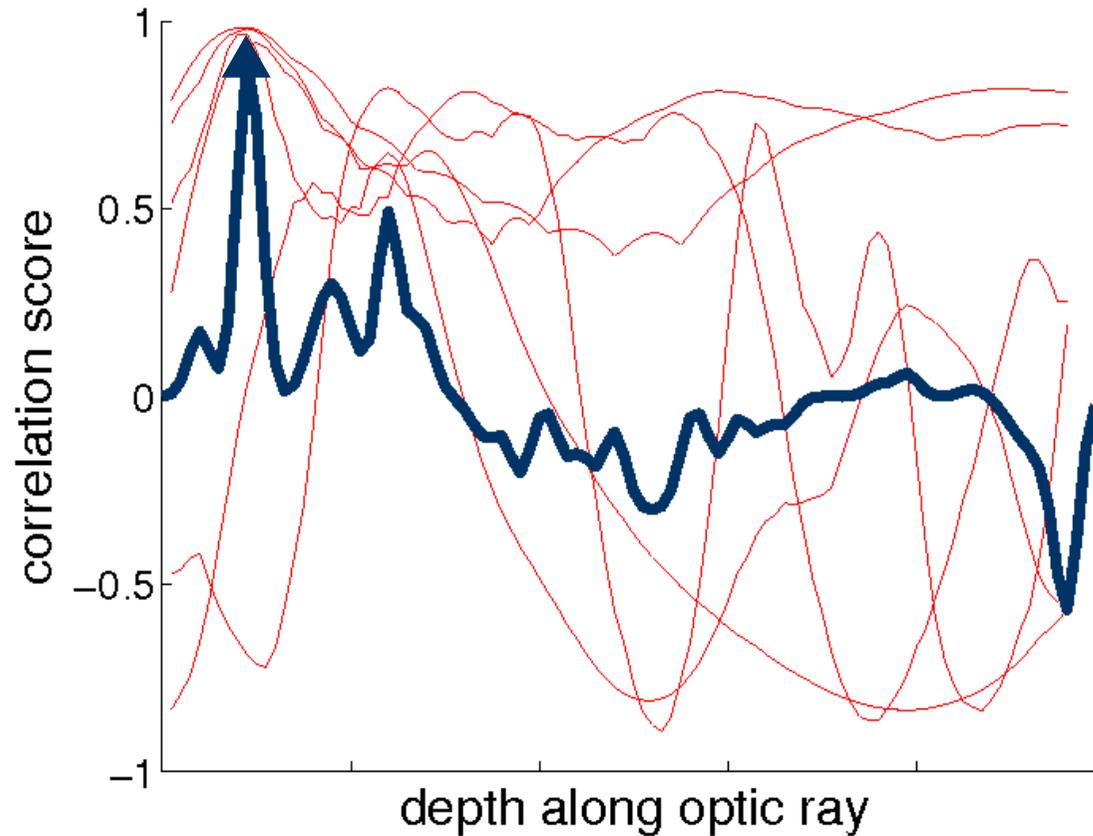
KEY assumption

the correct depth appears at a local maximum of matching score

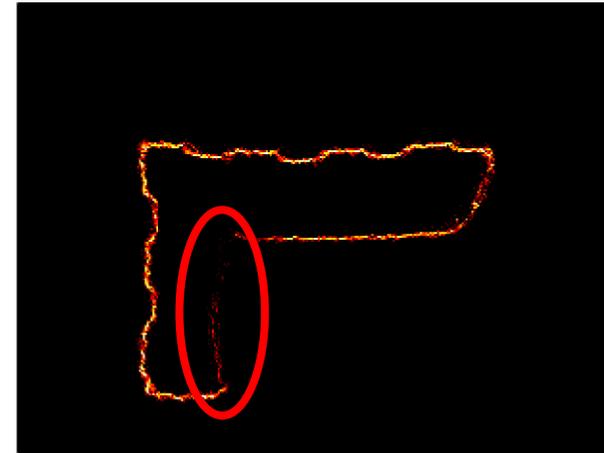
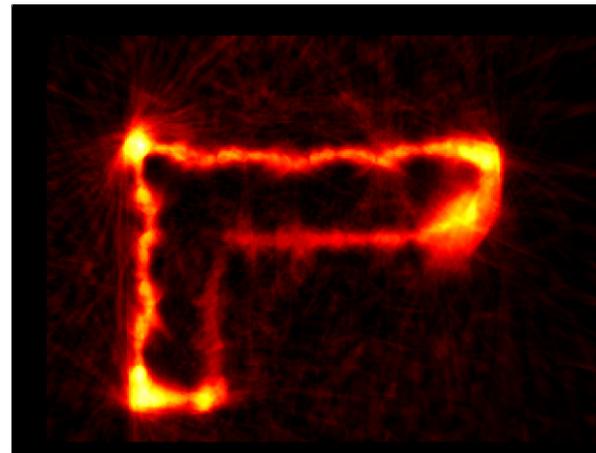
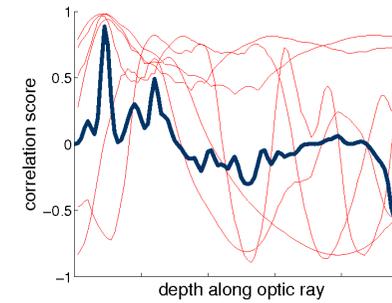
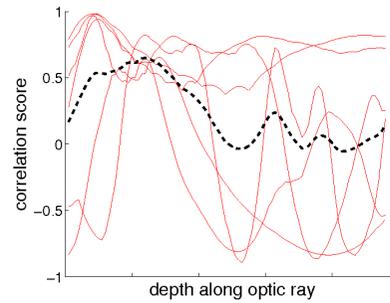
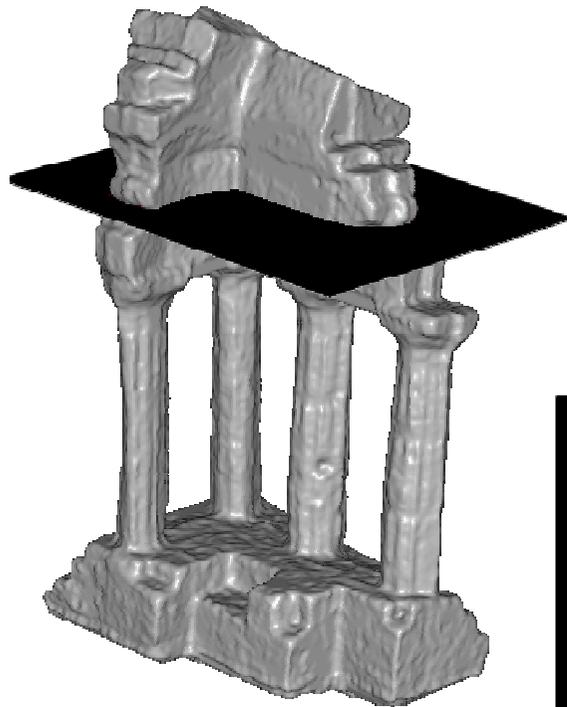


# Peaks of matching score

Parzen filter- sliding counter of local maxima



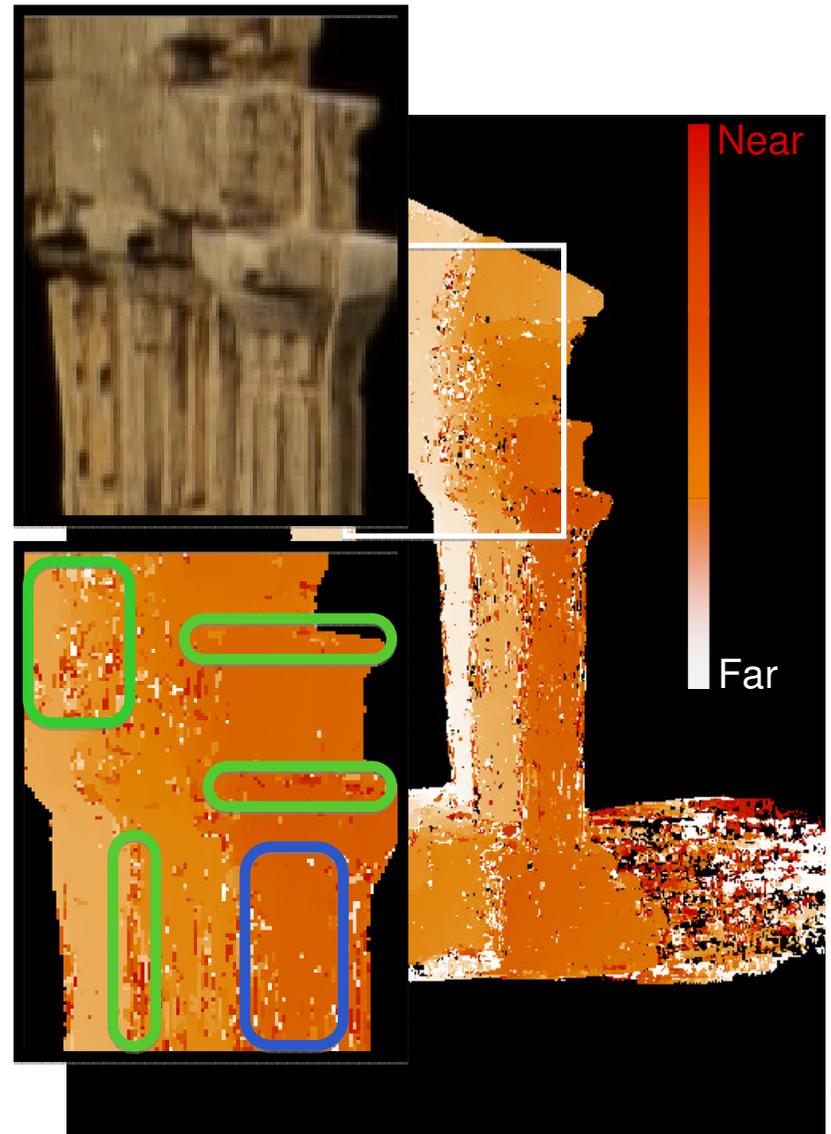
# Max of Parzen Filter Output



MATLAB

# Failure cases

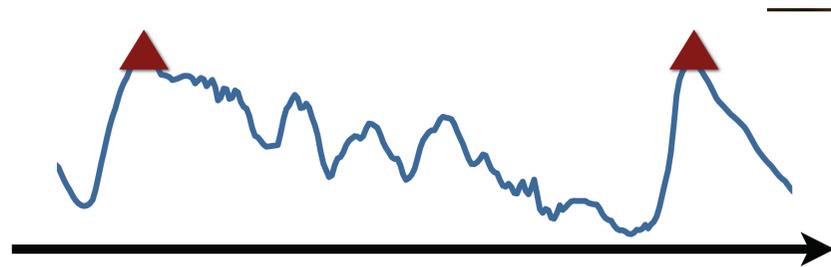
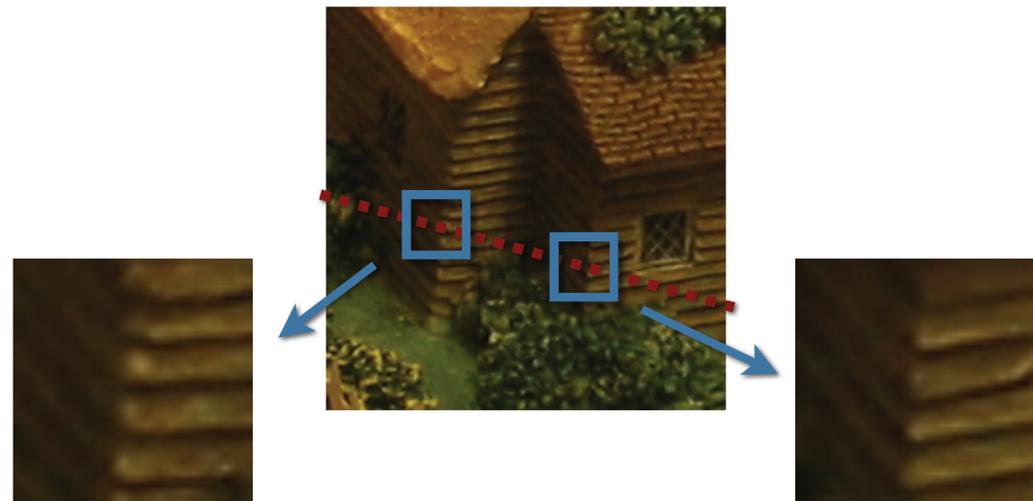
- Repeated Texture  
(match in incorrect location)
- Matching failure  
(surface not visible in one view, lack of texture, image noise etc)



# Repeated Texture



# Repeated Texture



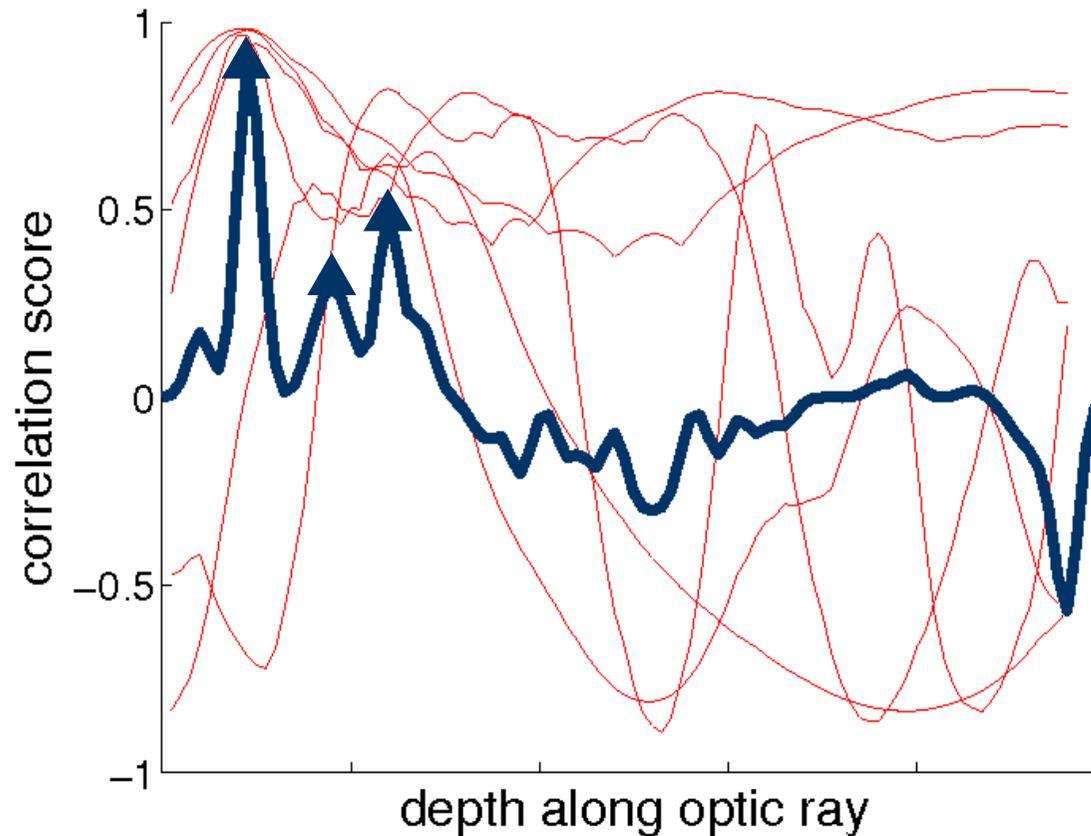
Correct depth can be found in **one** of the peaks

# Matching failure

- Due to
  - Occlusion
  - Window distortion
  - Image noise
  - Lack of texture
- NCC score is essentially a **random signal**

# Peaks of matching score

- All local maxima of Parzen filter output could be good hypotheses
- How do we pick right one?



# Exploit redundancy

- Two types of redundancy:
  - Depth of **neighbouring** pixels in **same** image
    - Depth of neighbours can provide support for the correct depth hypothesis
    - Useful in sparse sequences
  - Depth of **same** pixel in **neighbouring** images
    - If viewpoints are sufficiently close, correct depth hypothesis persists, incorrect is unstable.
    - Useful in dense sequences

# Exploit pixel neighborhoods

- Take the  $K$  top peaks of the **filter output** as depth hypotheses for each pixel. Additional hypothesis is “**unknown depth**”

$$k_i \in \{1 \dots K, \mathcal{U}\}$$

- Build a **2D discrete MRF** to select the appropriate peak

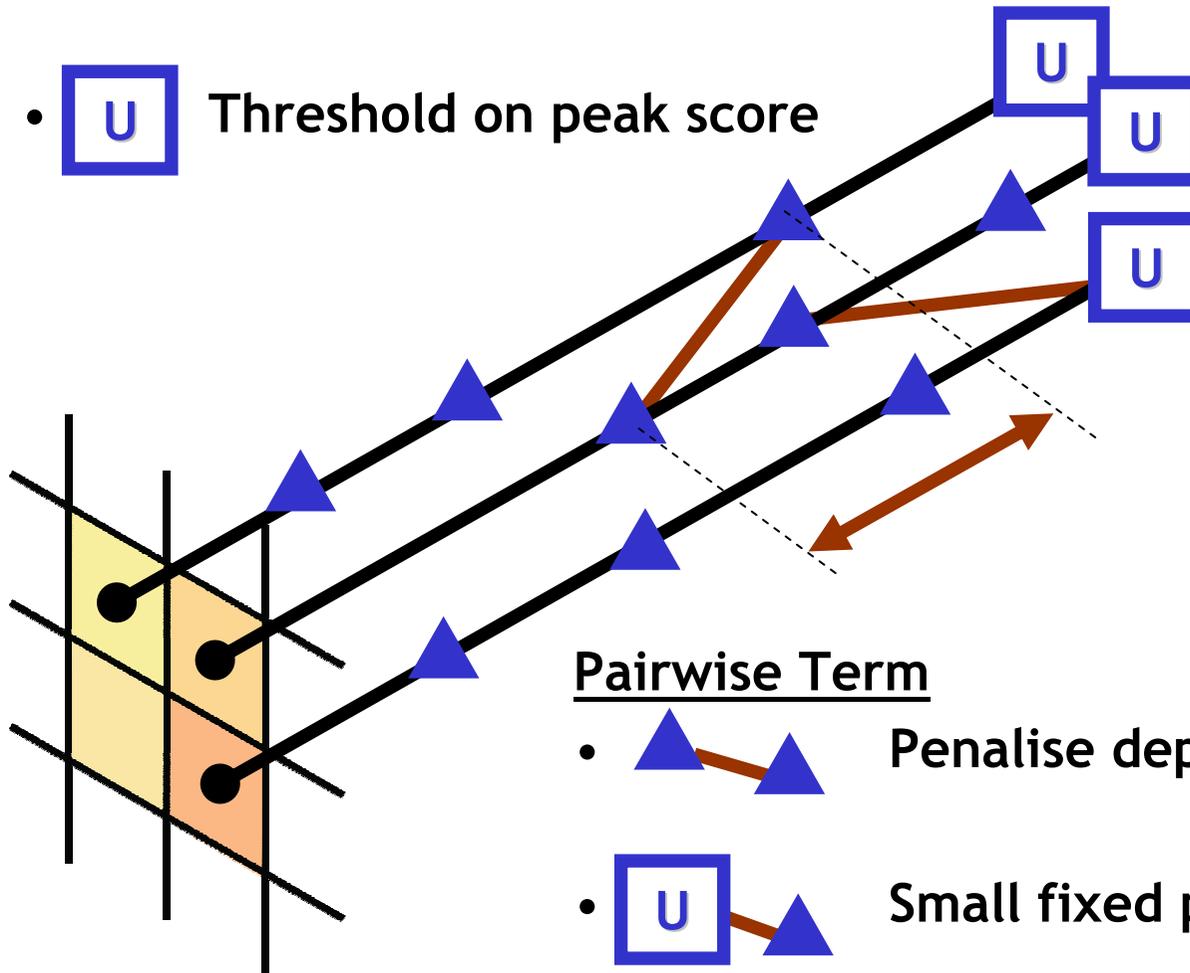
$$\sum_i \phi(k_i) + \sum_{(i,j)} \psi(k_i, k_j)$$

1. Unary energy  $\phi$ : bias depth towards **highest peaks**
  2. Pair wise energy  $\psi$ : encourage neighbour pixels to have **similar depths**
- Use “**unknown depth**” label for robustness against low scores or spatially inconsistent peaks
    - If one of the two neighbours is “unknown”, pair wise term is constant
    - Small penalty cost for “unknown” labels
  - MRF can be approximately solved using variety of solvers (TRW)

# MRF

## Unary Term

- ▲ Penalise peaks with low score
- □ U Threshold on peak score



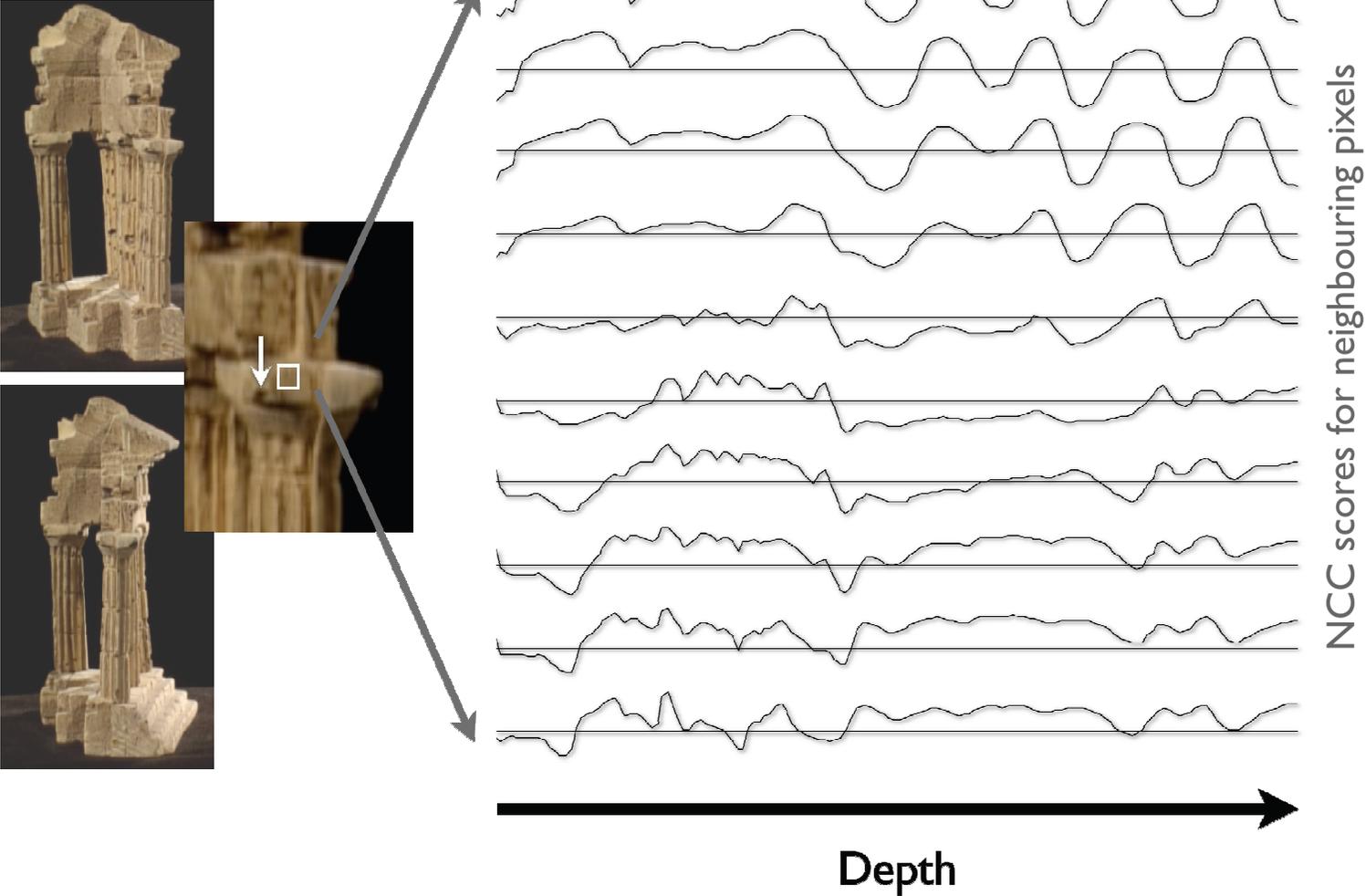
## Pairwise Term

- ▲ — ▲ Penalise depth disparity
- □ U — ▲ Small fixed penalty

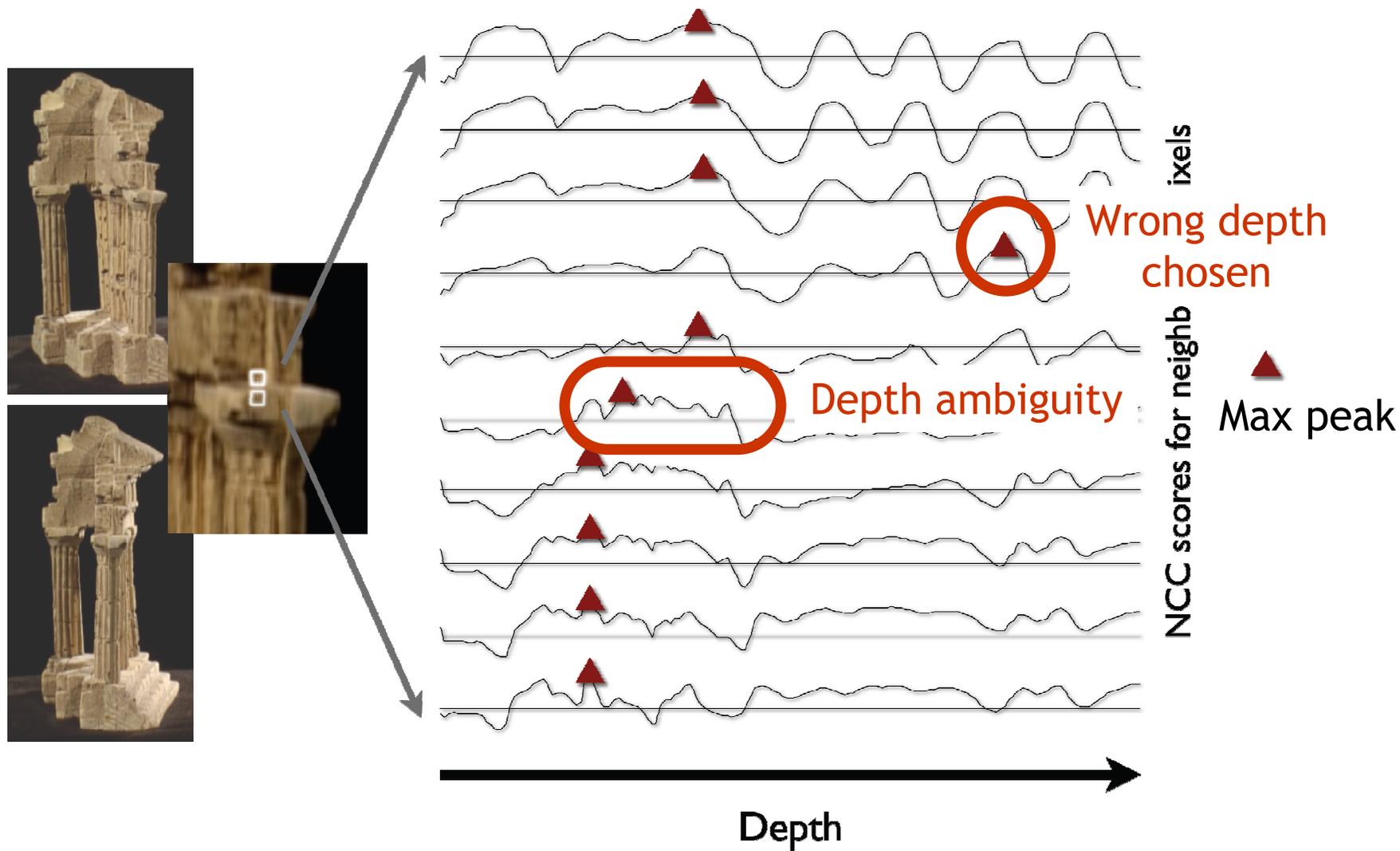
# Isn't this **early regularisation**?

- Yes...
  - ...but not so bad.
  - We merely **filter out** outlier measurements
  - If a pixel doesn't get support for any depth it becomes "unknown"
  - We are NOT **filling in** the data using a prior

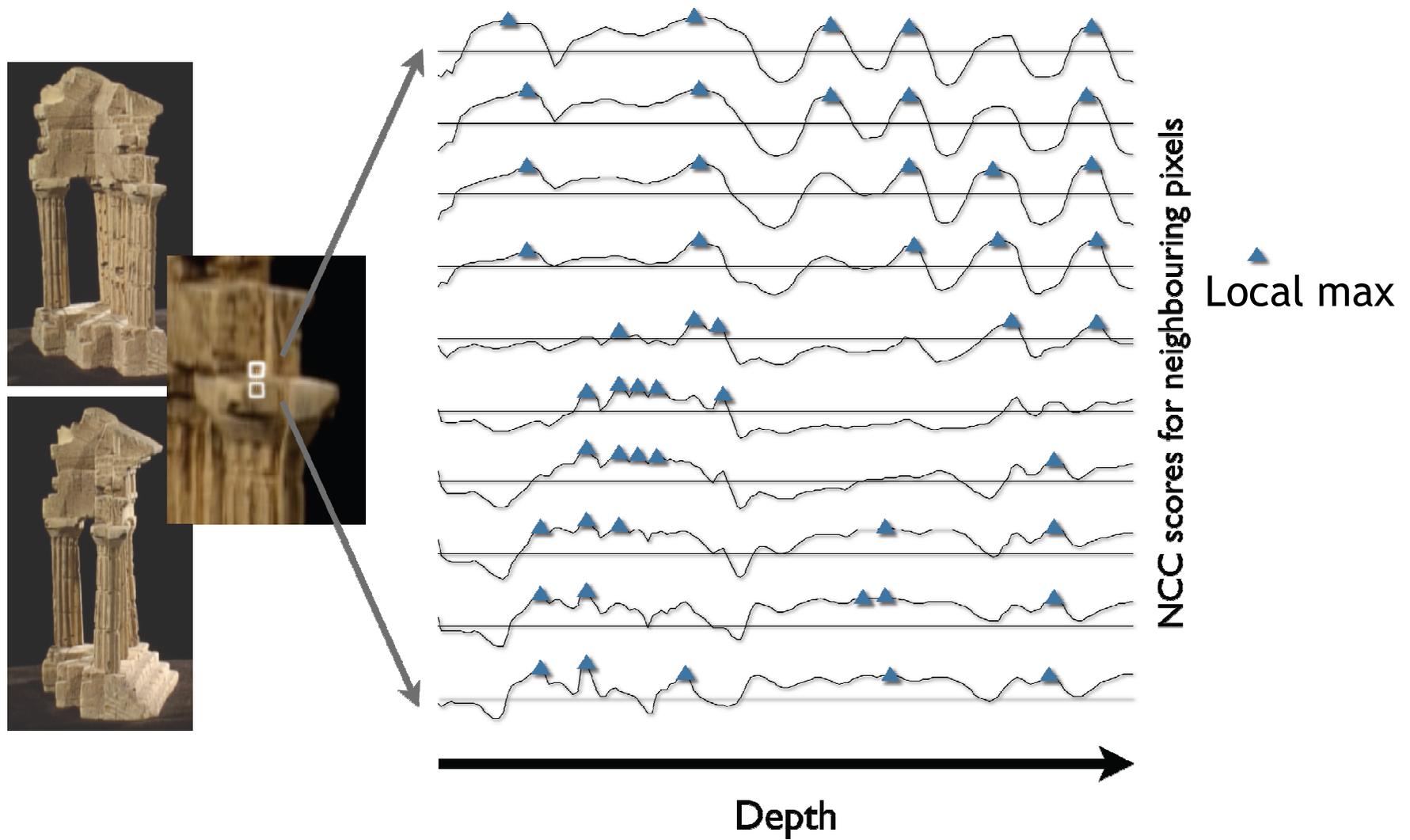
# Depth estimation



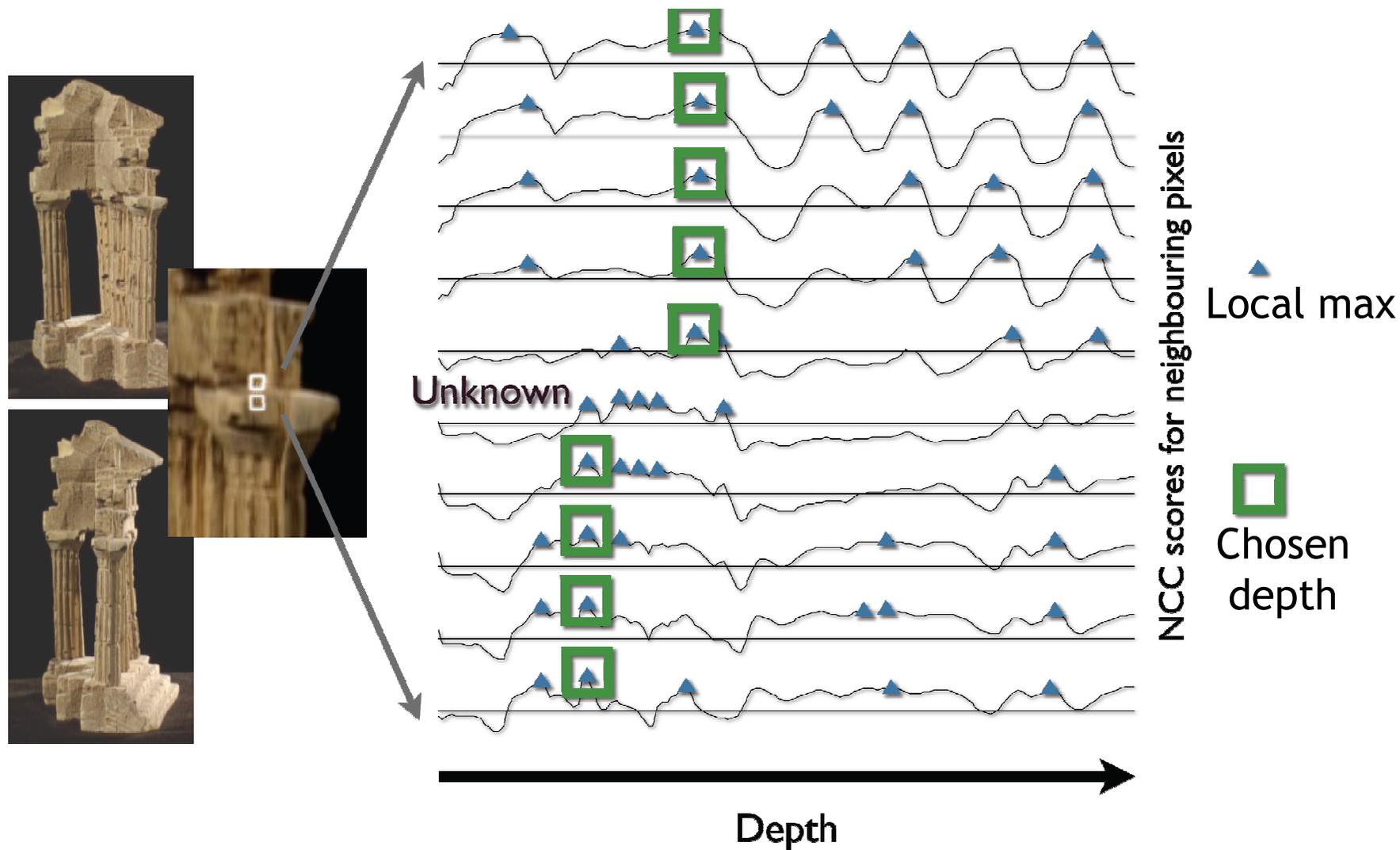
# Max peak

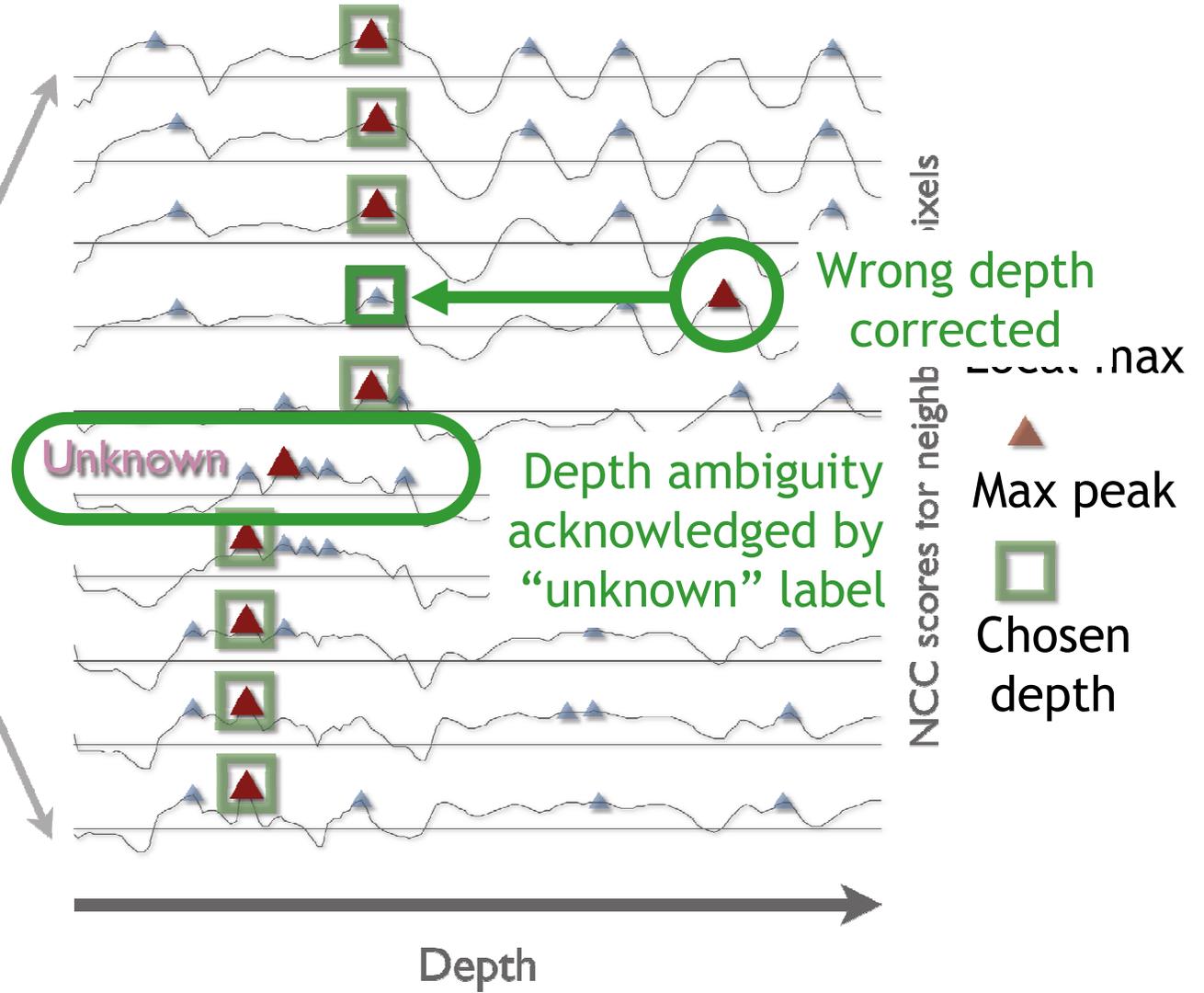


# K top peaks

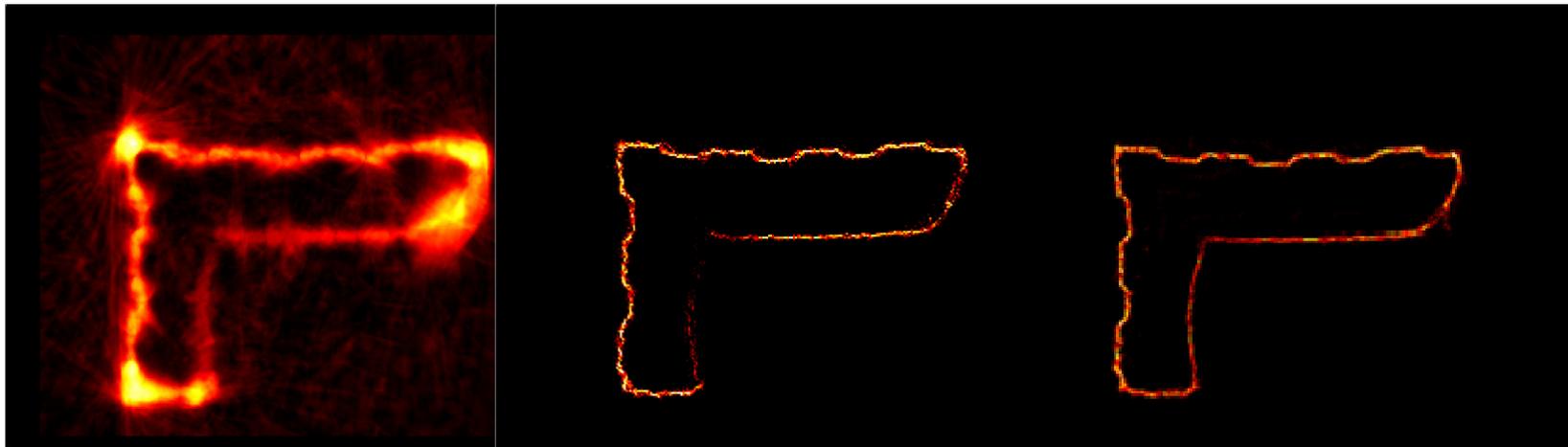
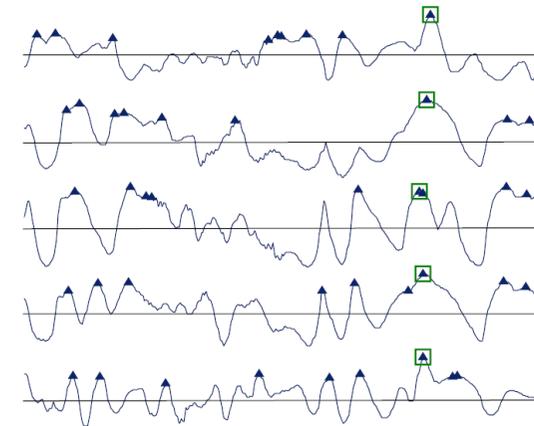
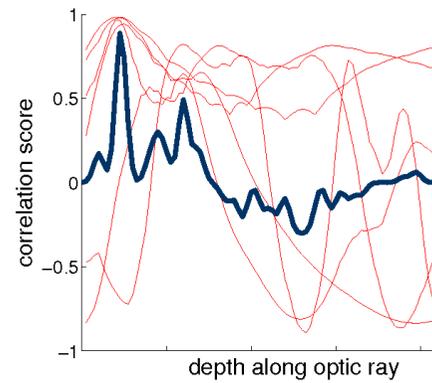
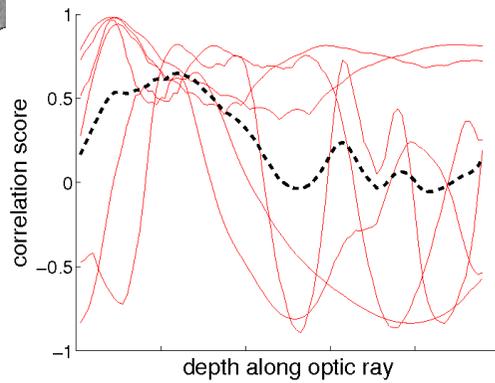
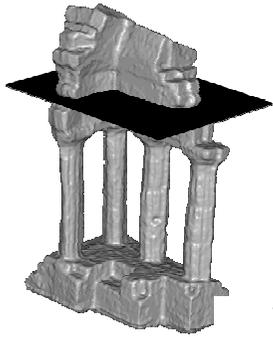


# After MRF filtering





# Multi-hypothesis MRF filtering

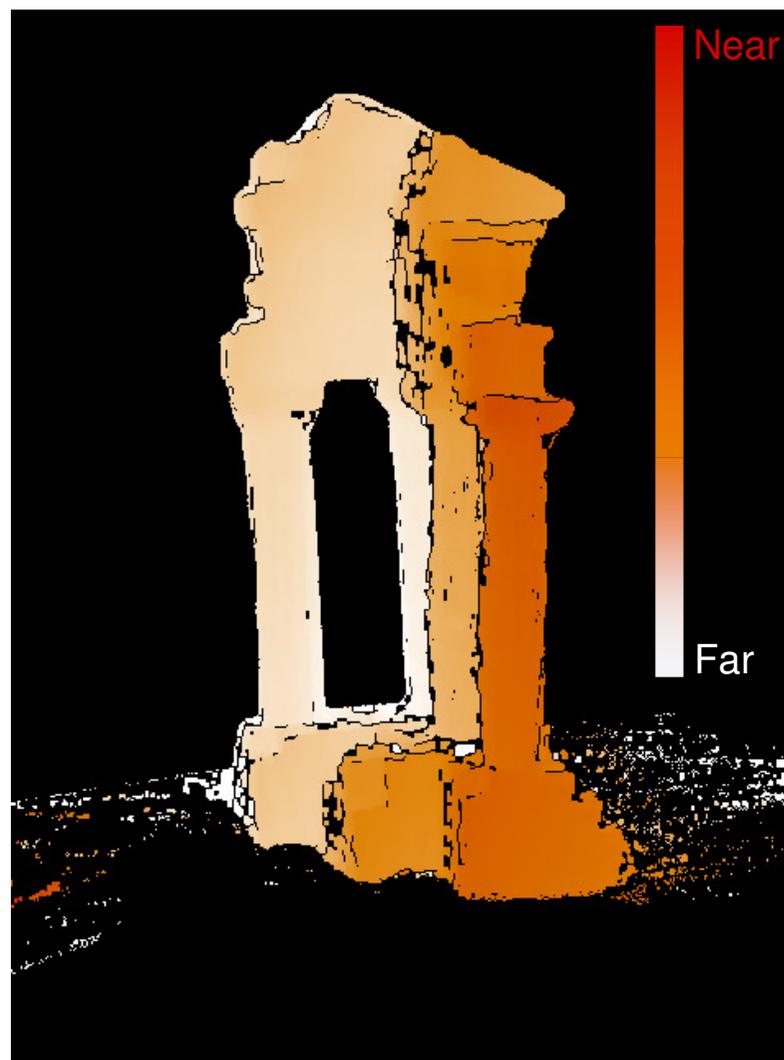


# Depth-Map Results

Taking the **maximum peak**



Results of the **MRF optimisation**

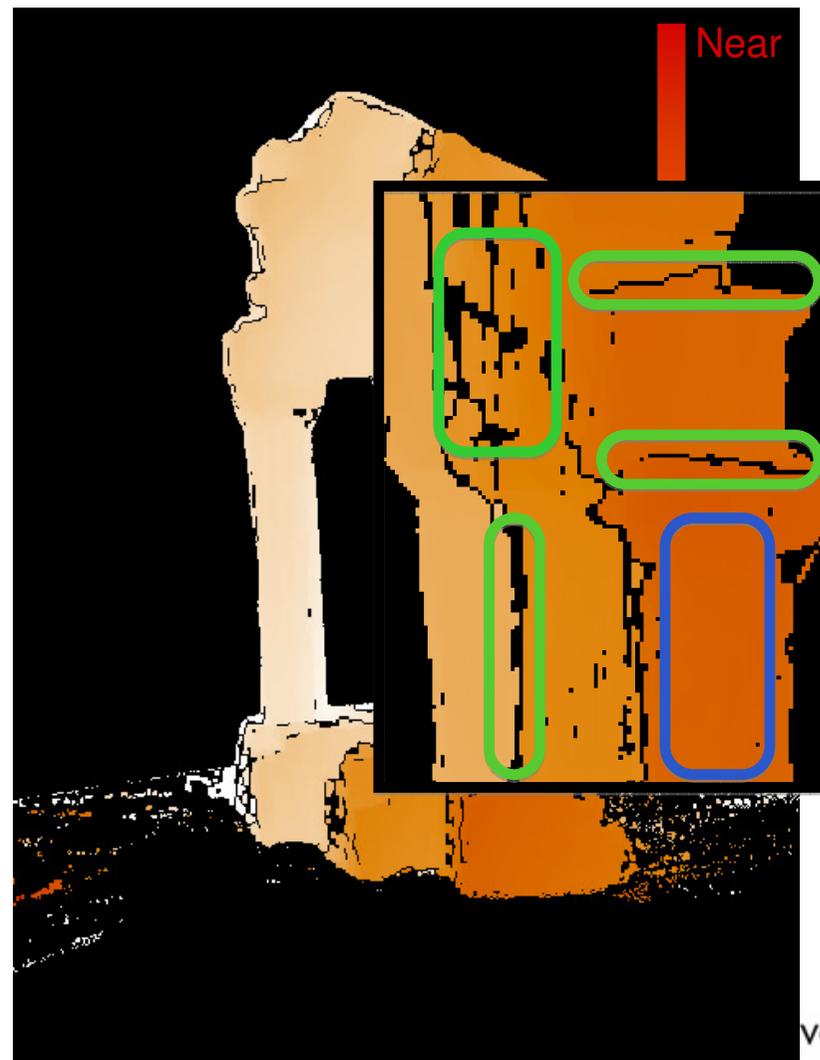


# Depth-Map Results

Taking the **maximum peak**

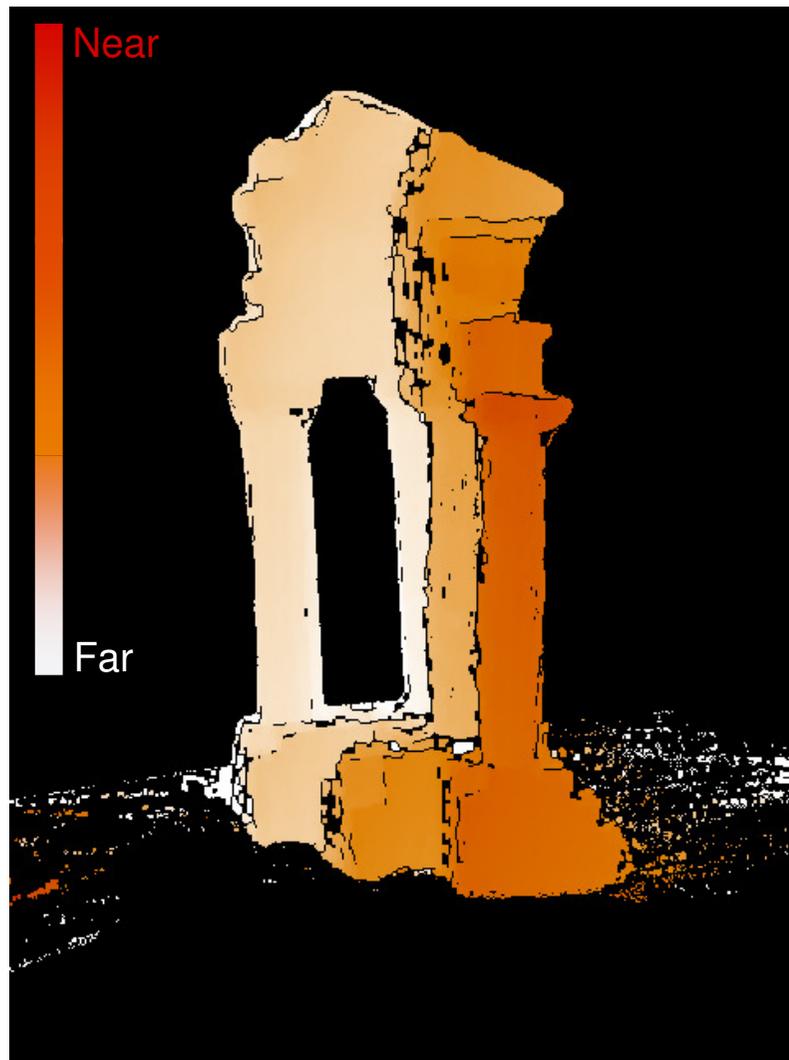


Results of the **MRF optimisation**

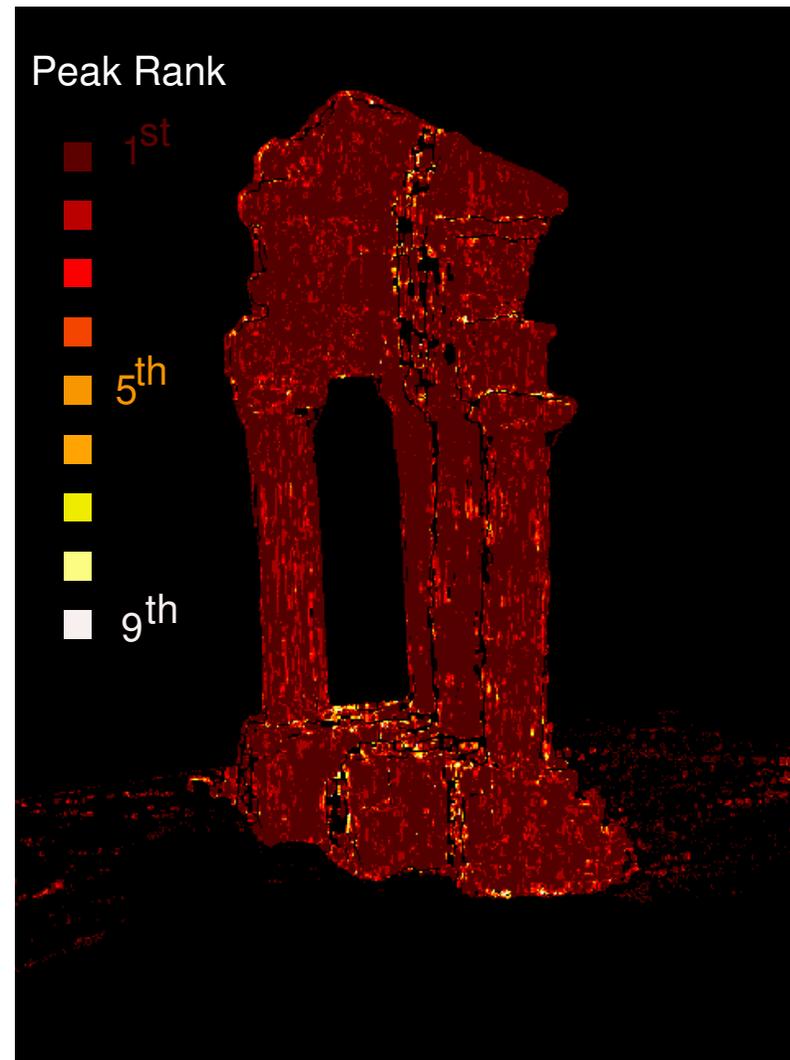


# Depth-Map Results

Results of the **MRF optimisation**

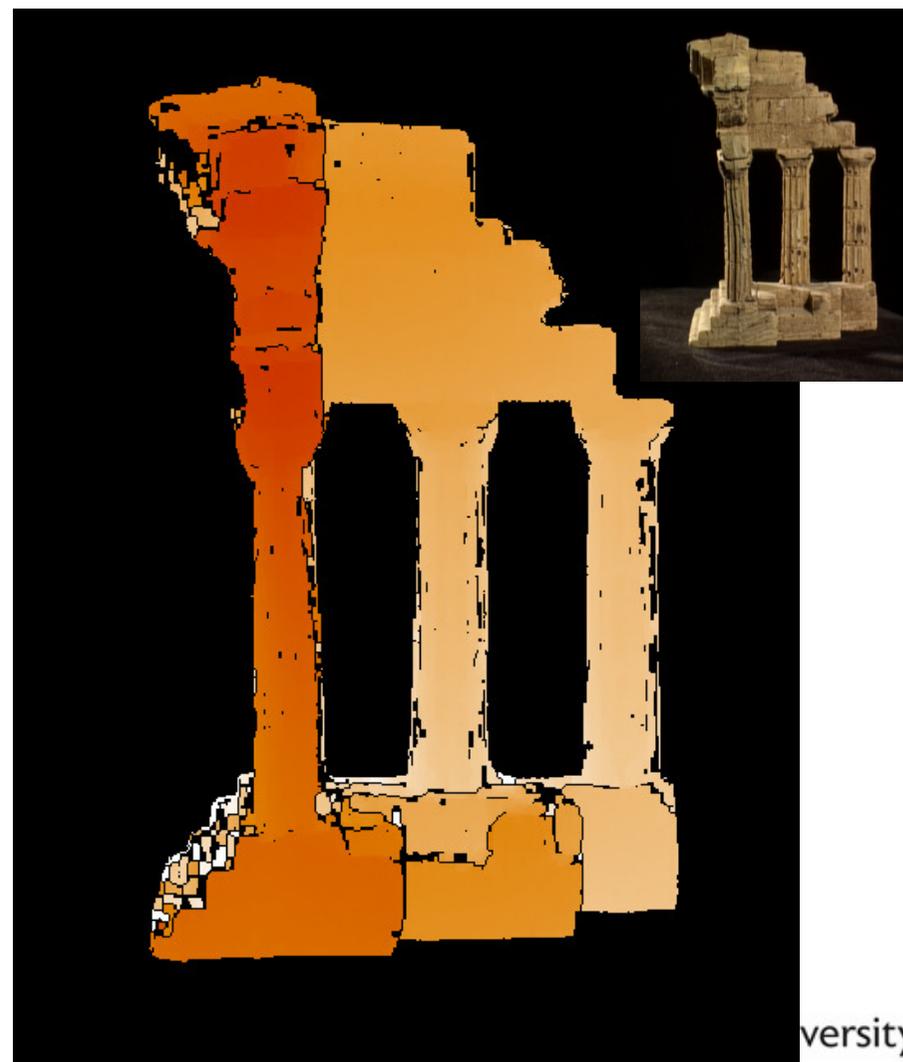


The **ranking** of the chosen peak



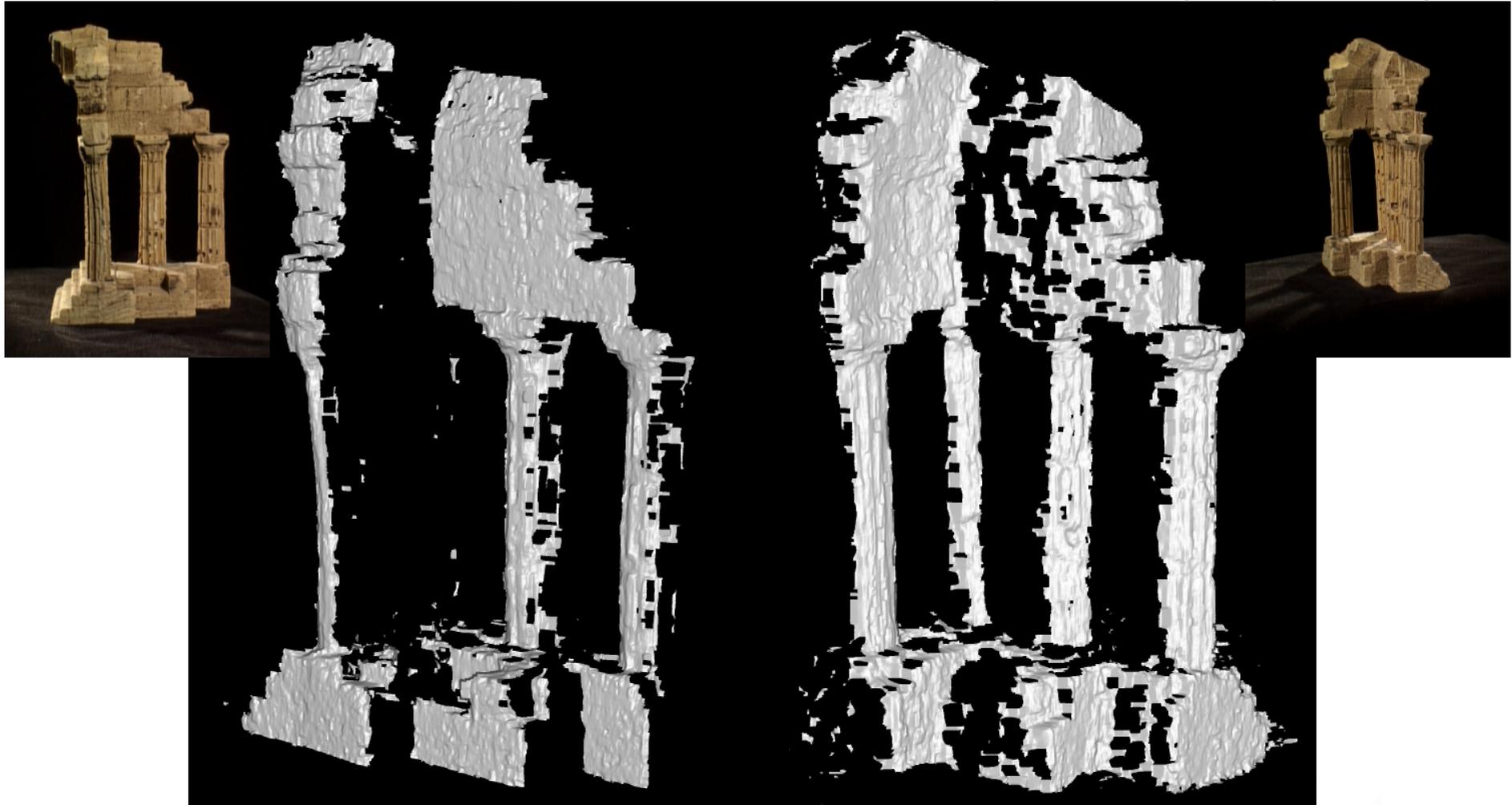
# Depth-Map Results

Results of the **MRF optimisation** for two neighbouring depth-maps



# Depth-Map Results

Results of the **MRF optimisation** for two neighbouring depth-maps



# Exploit redundancy

- Two types of redundancy:
  - Depth of **neighbouring** pixels in **same** image
    - Depth of neighbours can provide support for the correct depth hypothesis
    - Useful in sparse sequences
  - Depth of **same** pixel in **neighbouring** images
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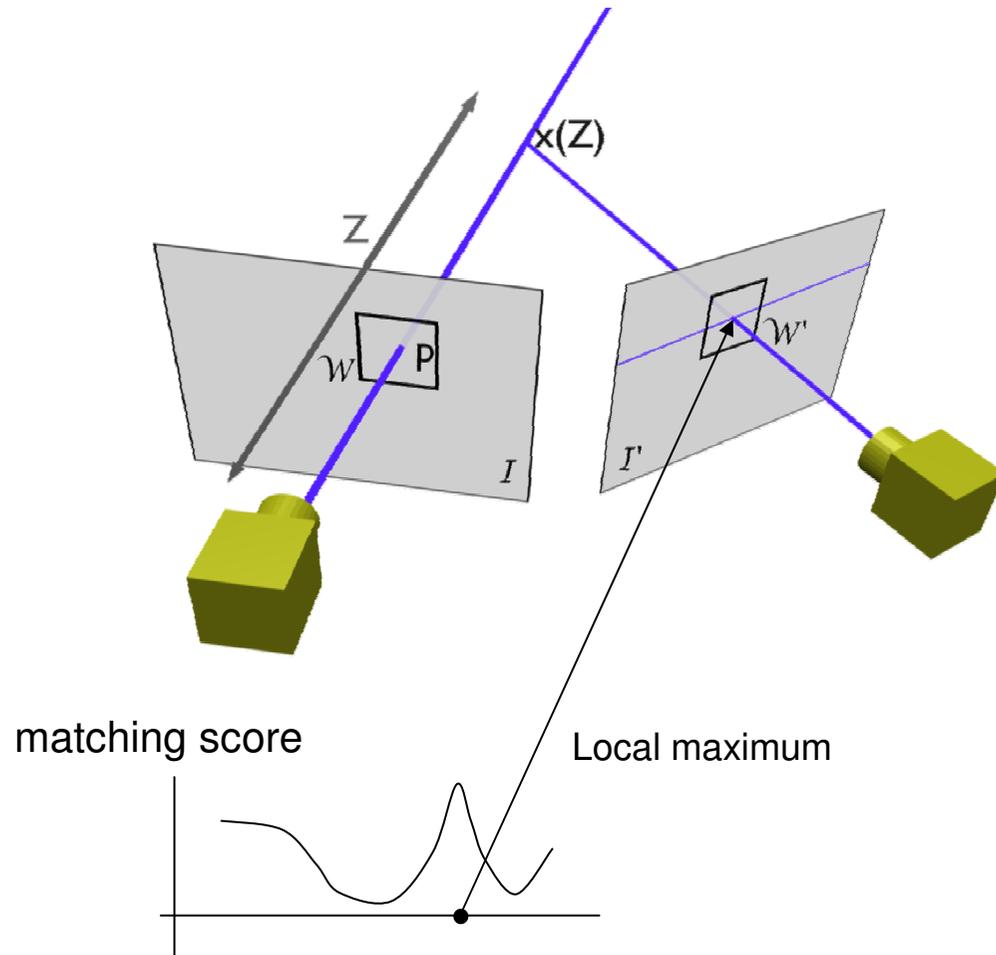
# Video-based Multi-View Stereo

- The correct depth appears at a local maximum of matching score
- With enough images, all ambiguities get resolved



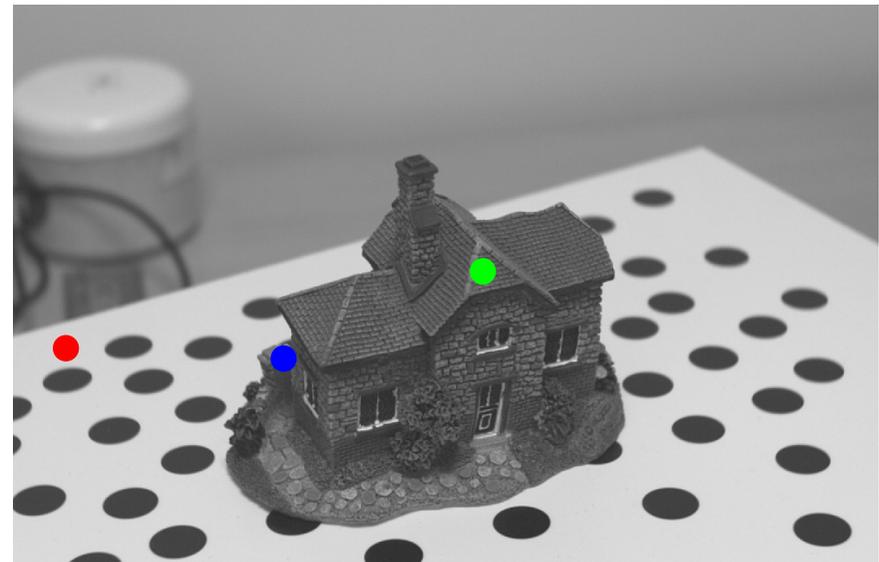
~600 frames

# Pixel = depth sensor

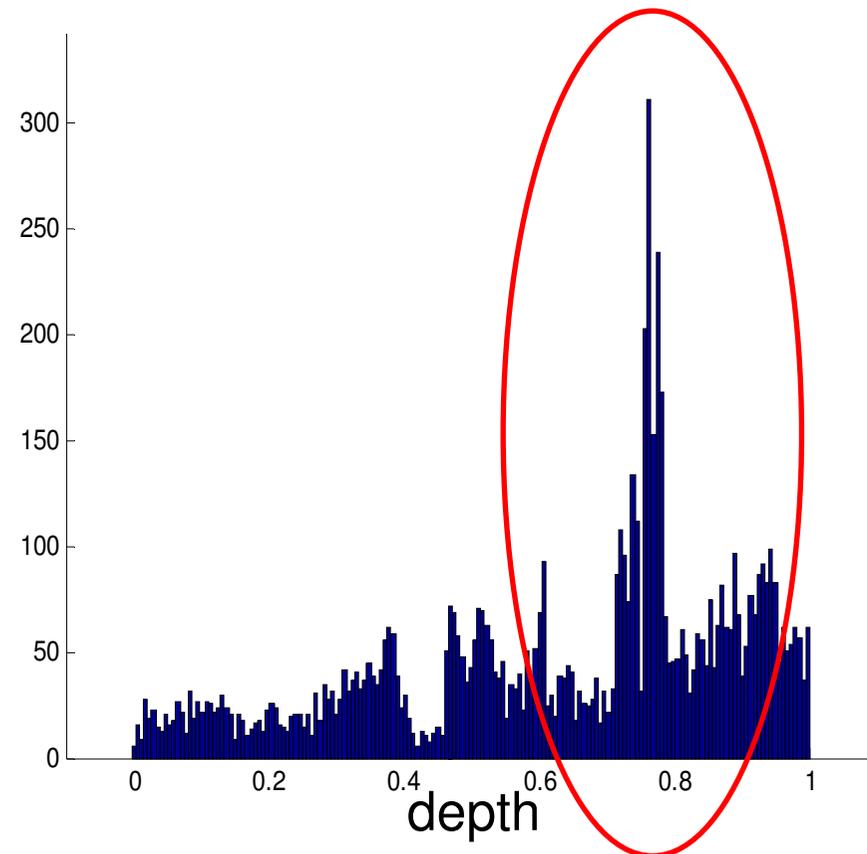


# What are the measurements like?

- Well textured pixel
- Untextured point
- Occluded point

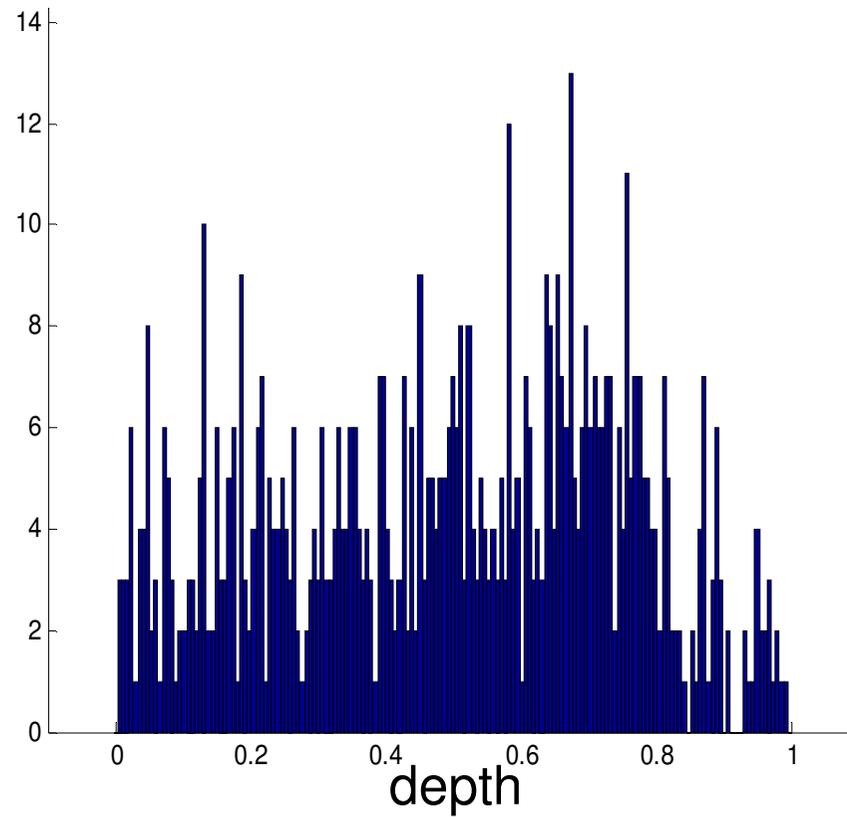


# Textured point

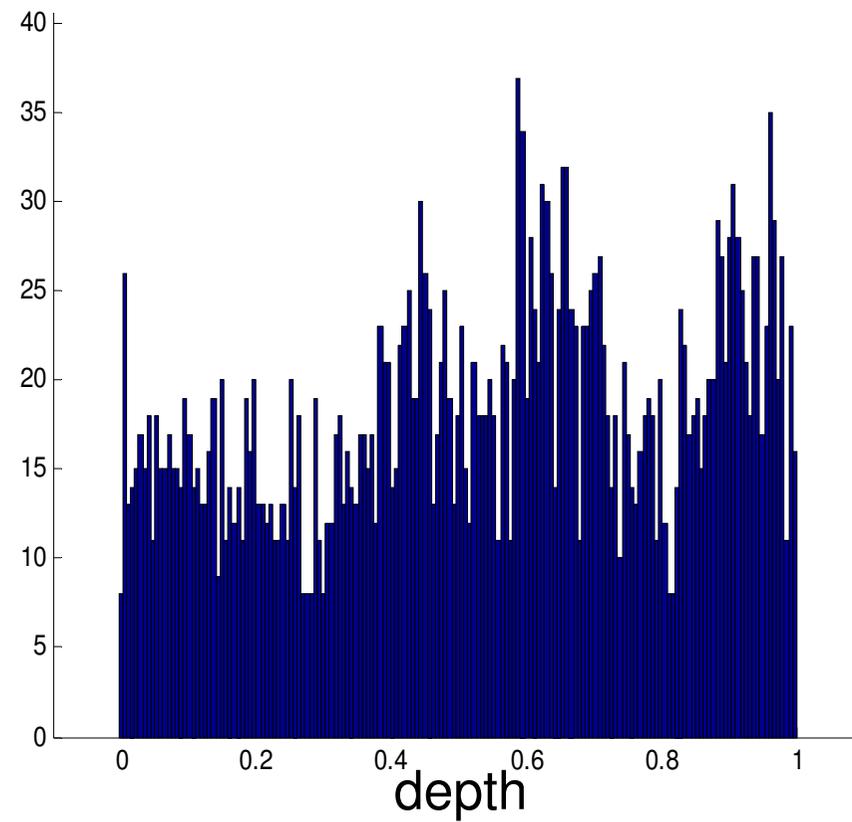


Clearly defined peak

# Untextured point



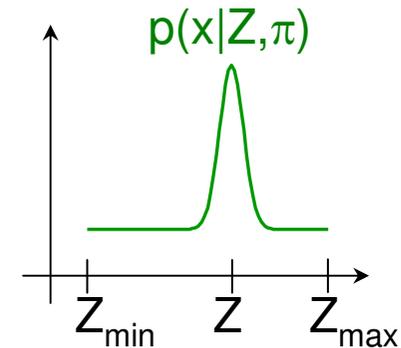
# Occluded point



# Strategy

- Model sensor probabilistically as a Gaussian+Uniform mixture

$$p(x|Z,\pi) = \pi N(x|Z,\tau^2) + (1-\pi) U(x,Z_{\min},Z_{\max})$$



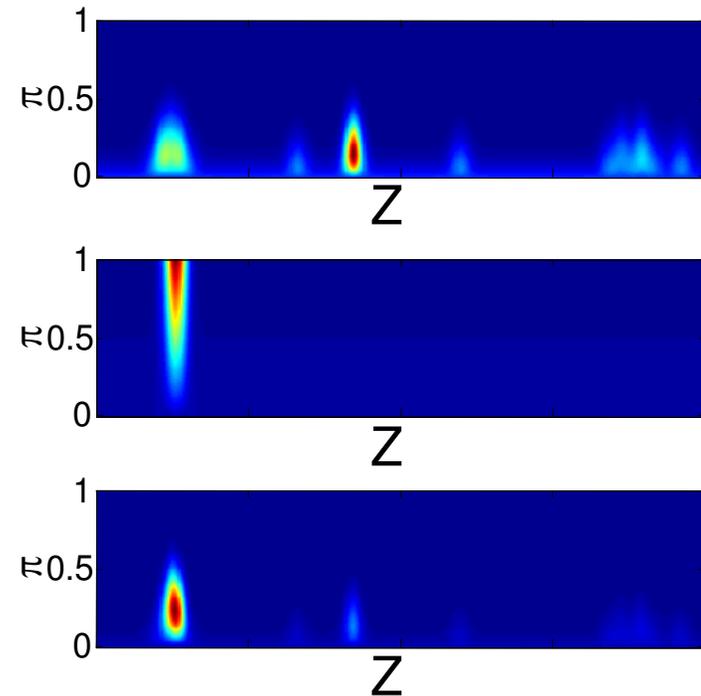
- $Z$  is the actual depth we are looking for
- $\tau^2$  is the variance of the sensor (1 pixel estimated from geometry of the problem)
- $Z_{\min}, Z_{\max}$  are the limits of the inference problem (bounding volume)
- $x$  is the measurement
- $\pi$  is the inlier ratio

# Strategy

- Large quantity of depth measurements  $x_1, \dots, x_t$  available
- We could get max likelihood solution for  $Z$  and  $\pi$  with EM, but **cannot afford EM for every pixel for every iteration**
- Particle filtering is **CPU intensive**
- Histograms are **memory intensive**
- Need *sequential inference* of
  - Depth of pixel,  $Z$
  - Inlier ratio for pixel,  $\pi$

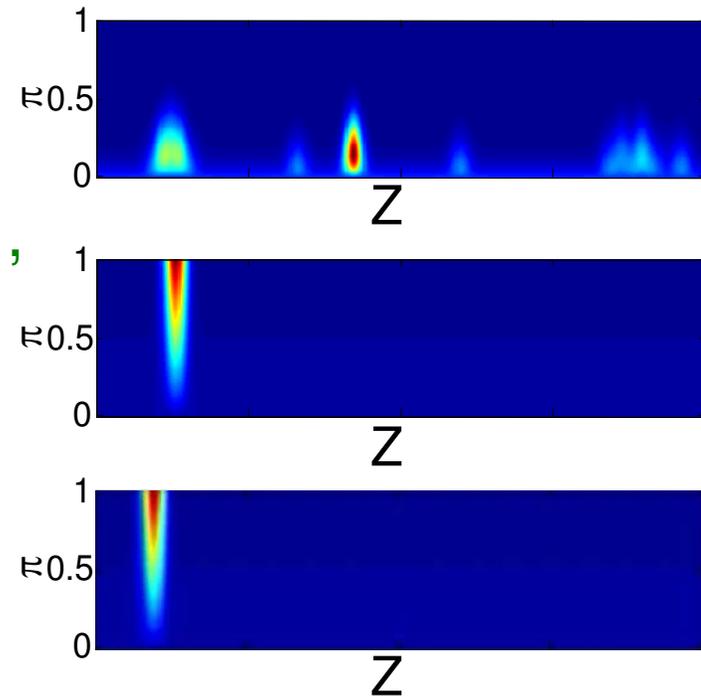
# Sequential inference

- Posterior at time  $t$ ,  
 $p_t(Z, \pi) := p(Z, \pi | x_1, \dots, x_t)$
- Likelihood of measurement at  $t+1$ ,  
 $p(x_{t+1} | Z, \pi)$
- Posterior at time  $t+1$ ,
  - $p_{t+1}(Z, \pi) \propto p(x_{t+1} | Z, \pi) \times p_t(Z, \pi)$
- What form can  $p_t(Z, \pi)$  take?
  - Non-parametric 2d histogram is too expensive
  - Can we approximate with a parametric form?



# Sequential inference

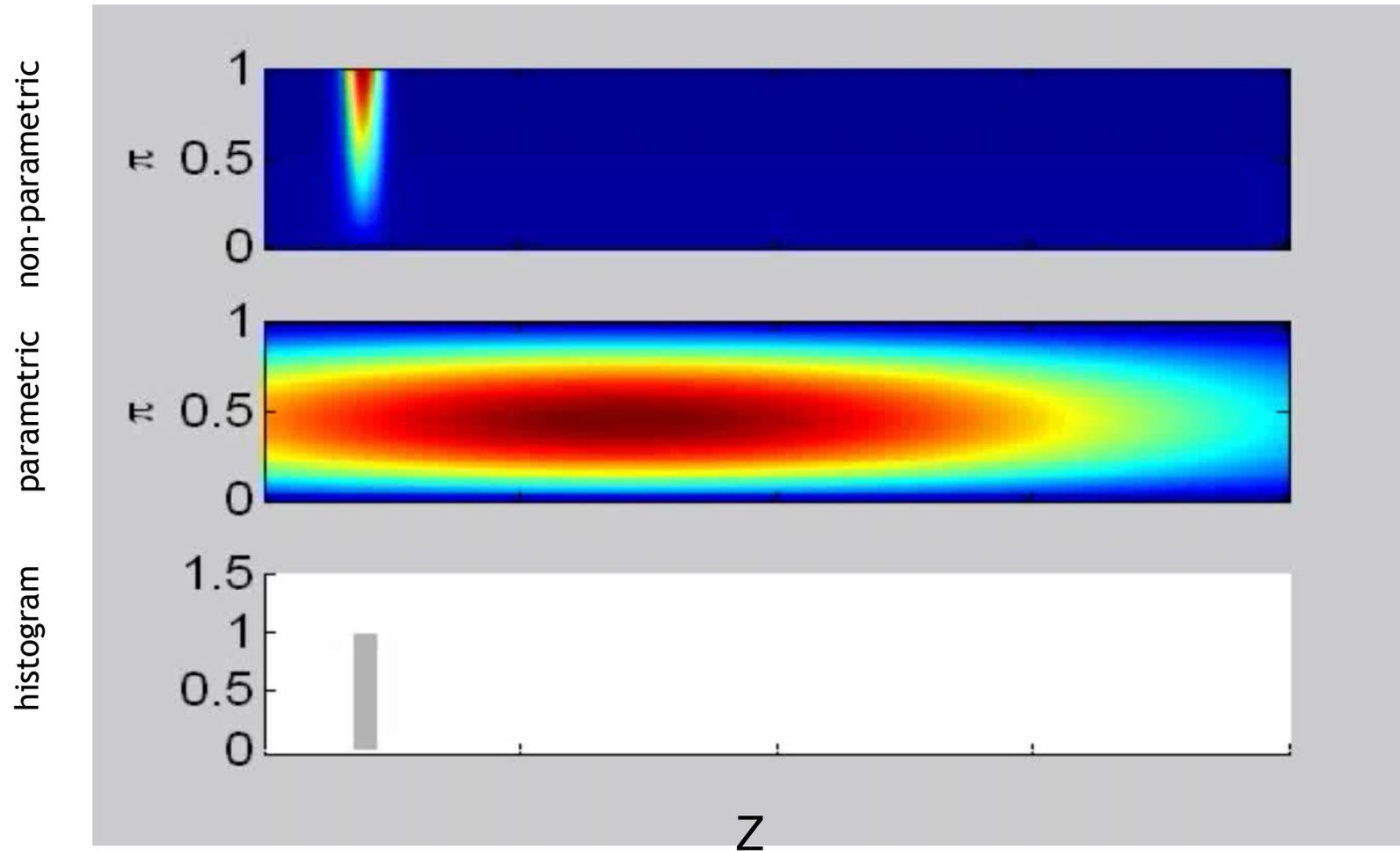
- **Posterior** at time  $t$ ,  
 $p_t(Z, \pi) := p(Z, \pi | x_1, \dots, x_t)$
- **Likelihood** of measurement at  $t+1$ ,  
 $p(x_{t+1} | Z, \pi)$
- **Posterior** at time  $t+1$ ,
  - $p_{t+1}(Z, \pi) \propto p(x_{t+1} | Z, \pi) \times p_t(Z, \pi)$
- What form can  $p_t(Z, \pi)$  take?
  - Non-parametric 2d histogram is too expensive
  - Can we approximate with a parametric form?



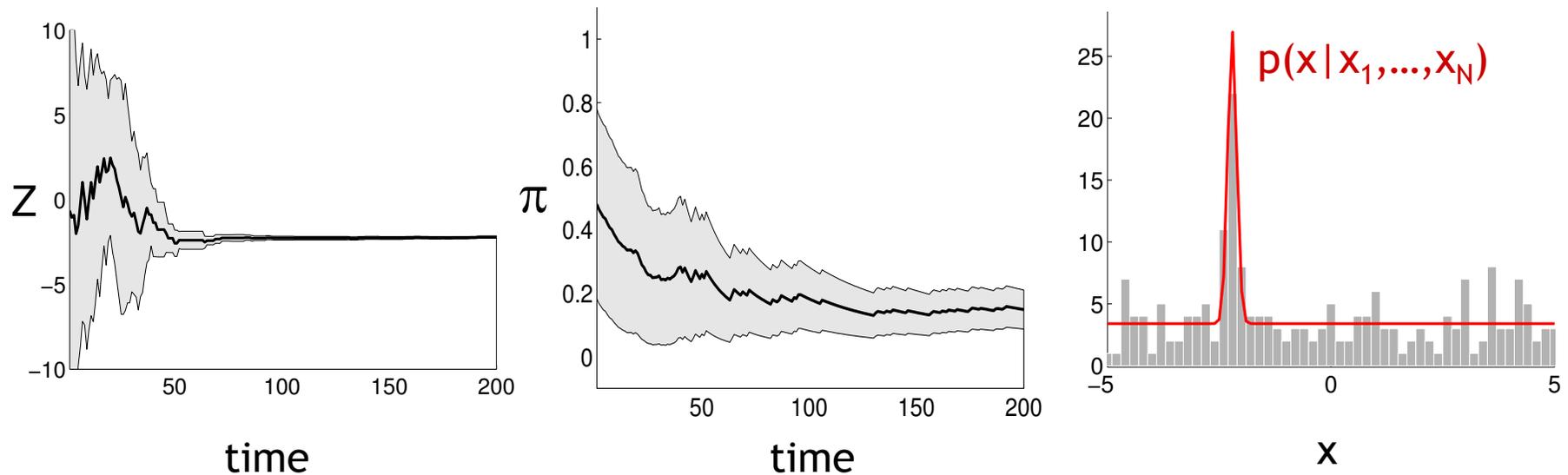
# Parametric posterior

- Maintain a posterior of the form
  - $p_t(Z, \pi) = \text{Beta}(\pi | a_t, b_t) \times N(Z | \mu_t, \sigma_t)$  Posterior represented with 4 numbers
  - Unimodal
  - Beta models random variable in  $[0, 1]$
- Use moment matching to obtain  $p_{t+1}(Z, \pi)$  from  $p_t(Z, \pi)$  and  $p(x_{t+1} | Z, \pi)$

# How well does it work?

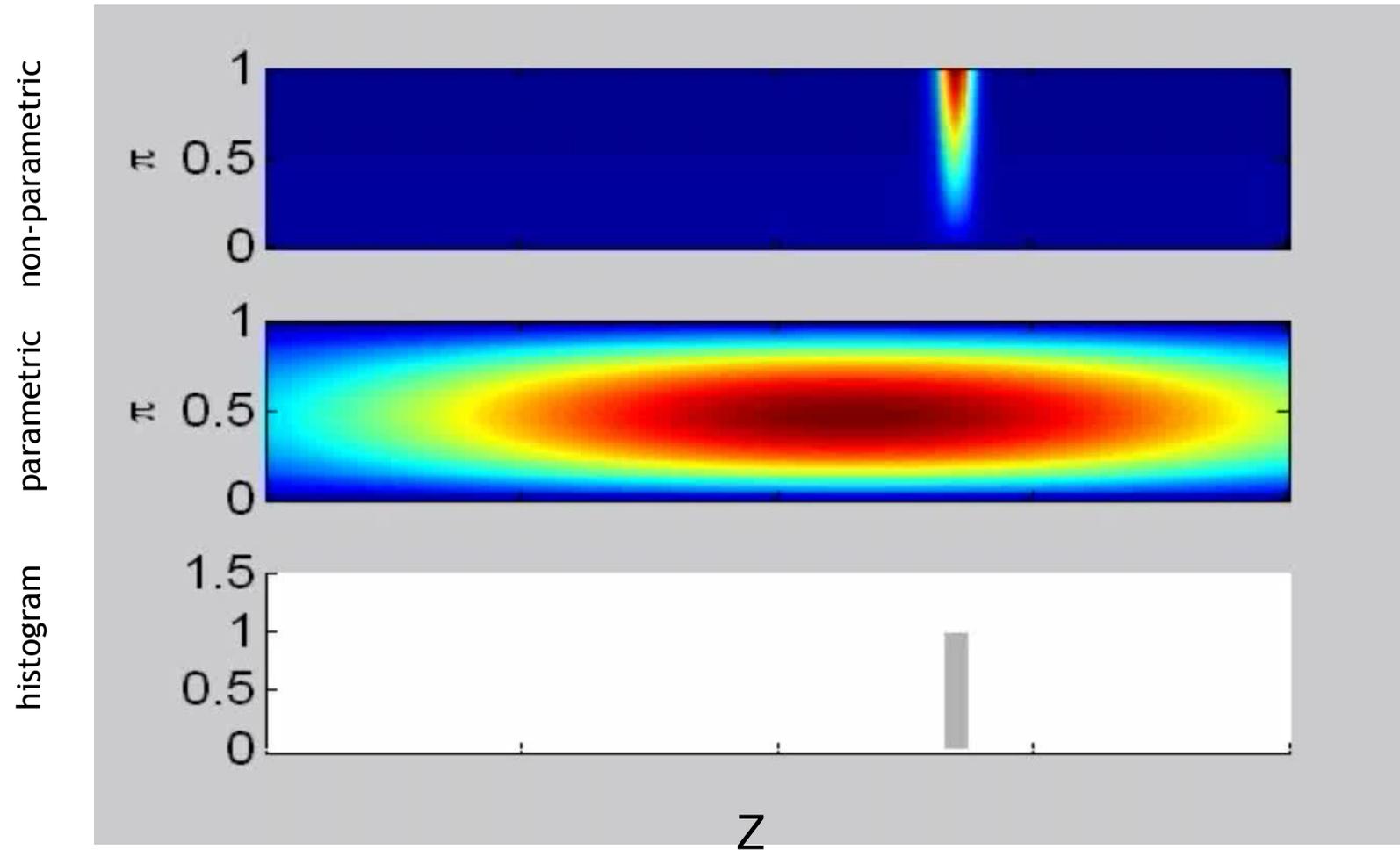


# Evolution of estimates



Intervals are two standard deviations either side away from the mean

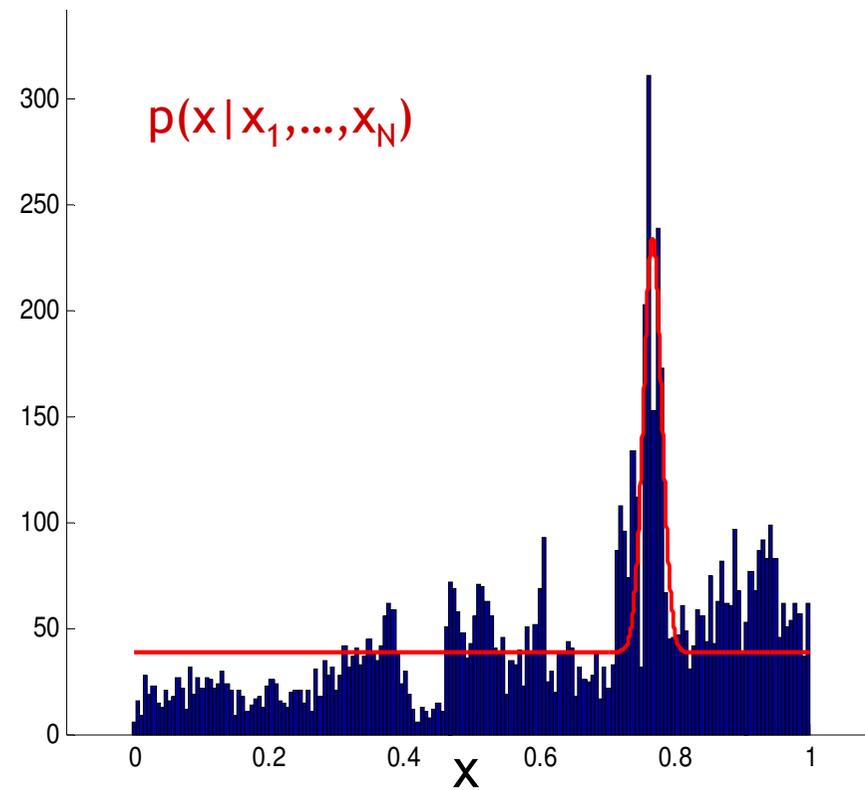
# Failure case of parametric posterior



# Textured point



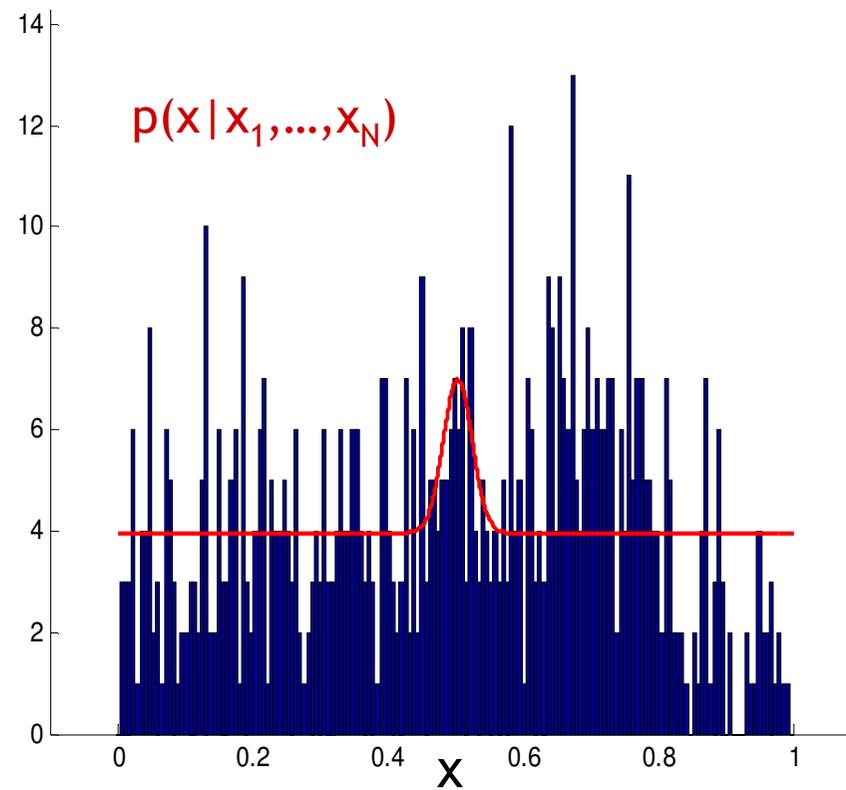
$\pi = 14.5\%$



# Untextured point



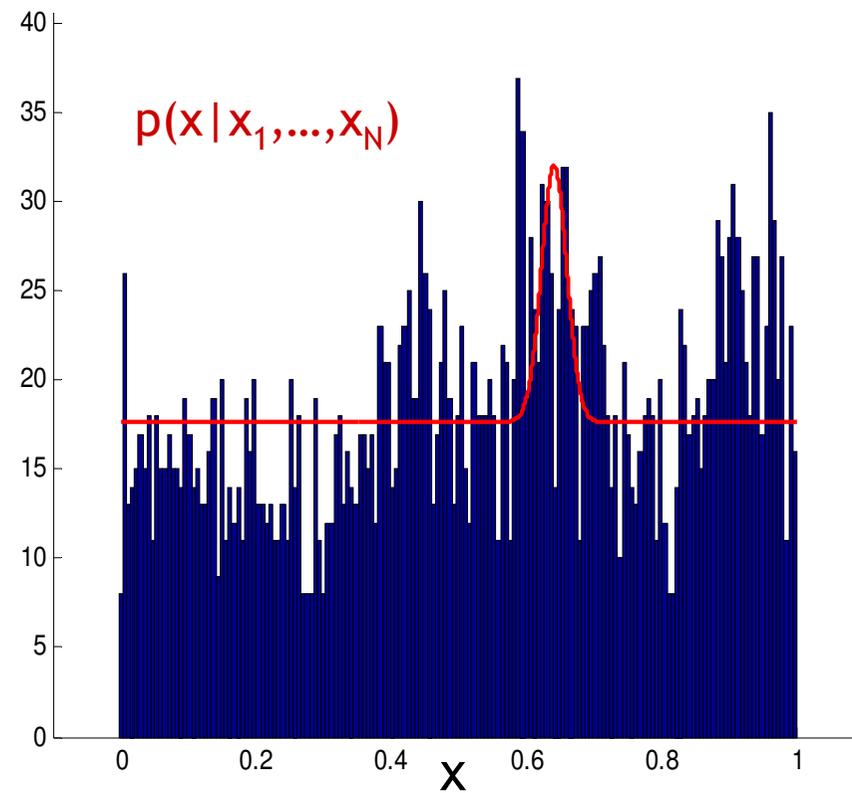
$\pi = 3.7\%$



# Occluded point



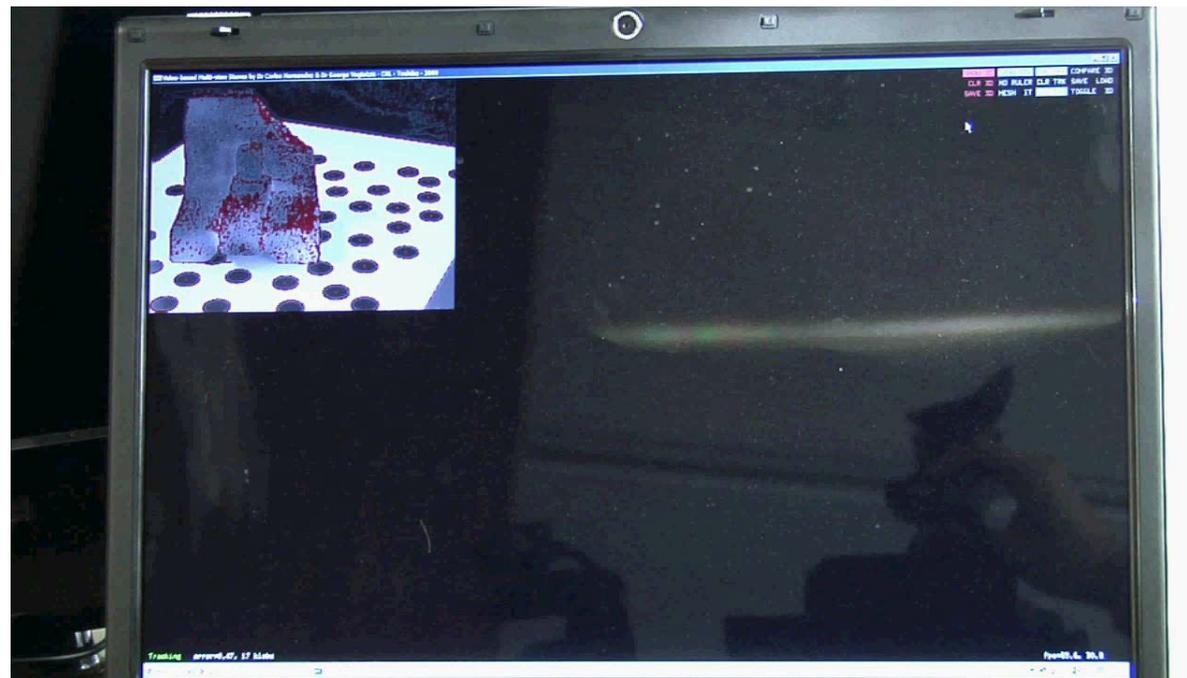
$\pi = 3.4\%$



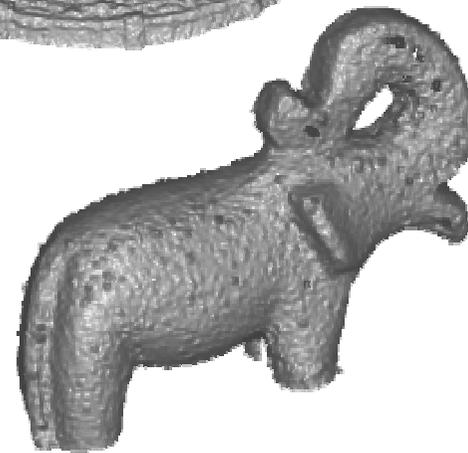
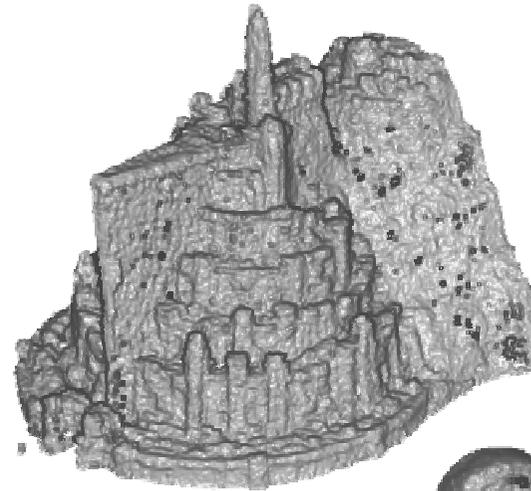
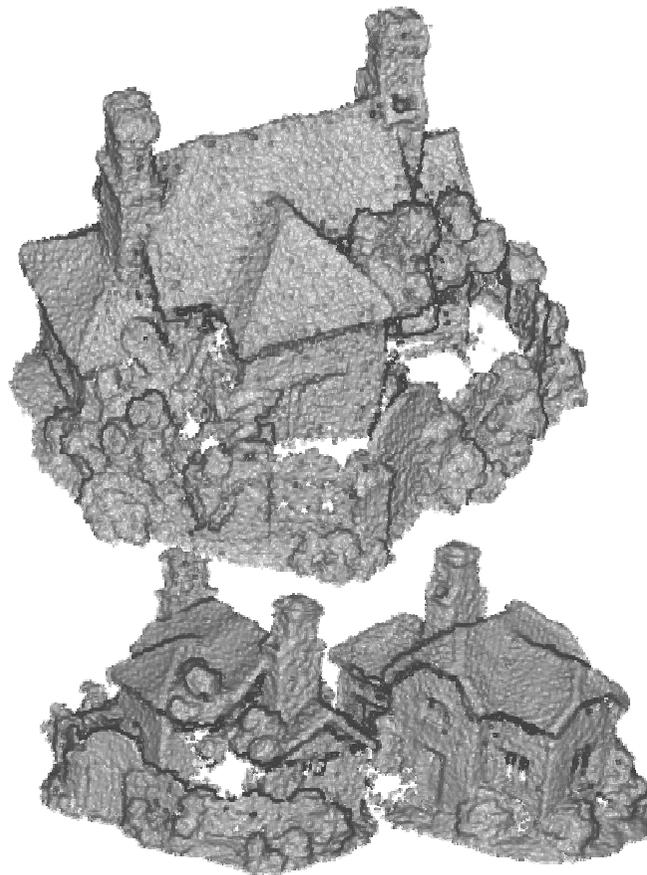
# Interactive Multi-view stereo

Benefits:

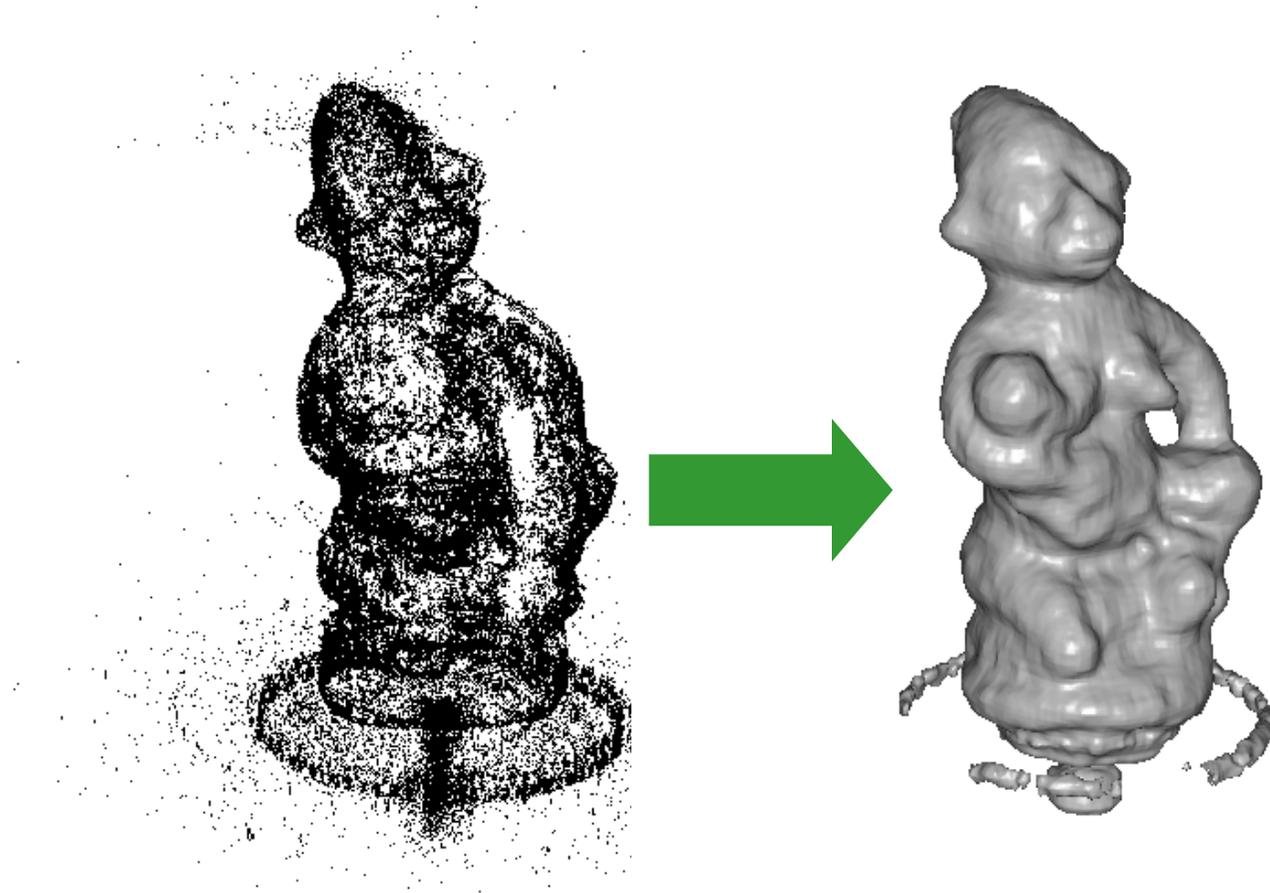
- Faster
- Feedback leads to better models
- Still passive & cheap



# Some reconstructions



# 3. Extract surface

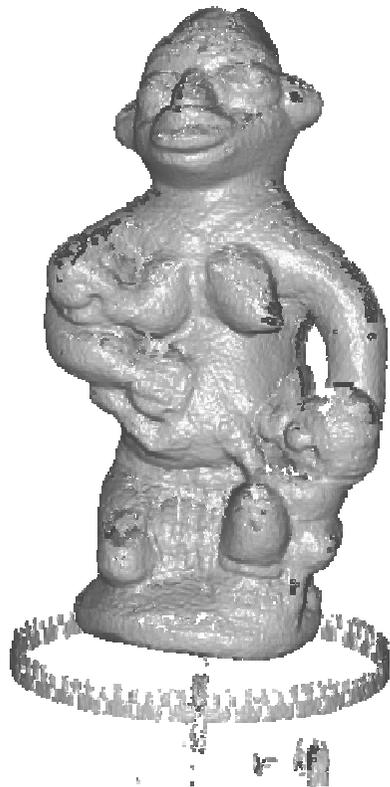


- 3d deformable meshes
- Graph-cuts
- Continuous convex optimisation

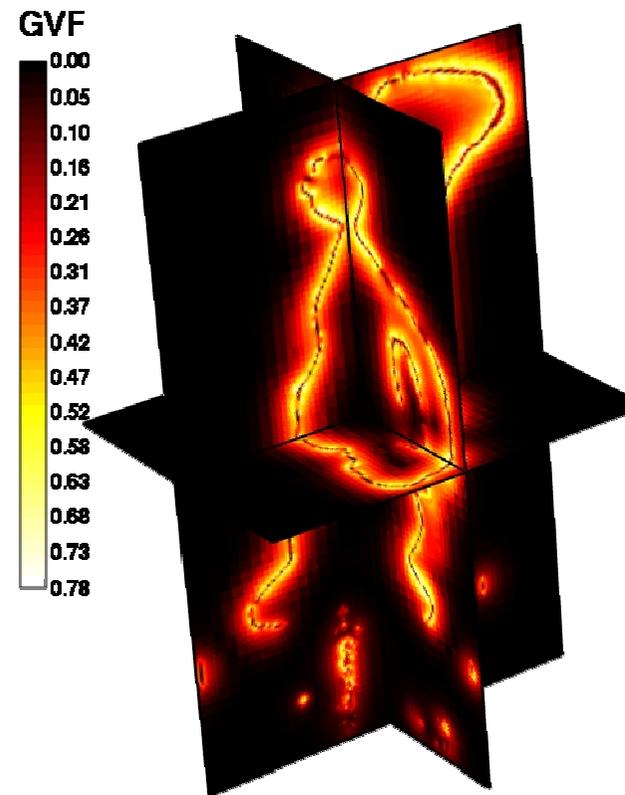
# 3D deformable meshes

- Effectively gradient descent
  - moving mesh towards photo-consistent locations
  - Smoothing at every iteration
    - $V_{t+1} := V_t + \alpha F_{\text{data}} + \beta F_{\text{regularisation}}$
- Advantages:
  - Fine control of the surface
  - First order (Laplacian) and second order (biharmonic) regularisation schemes available
  - Multiple clues can be fused easily, e.g. shading
- Cons:
  - Global convergence is **not** guaranteed
  - Difficult to cope with topology changes

# Improving convergence

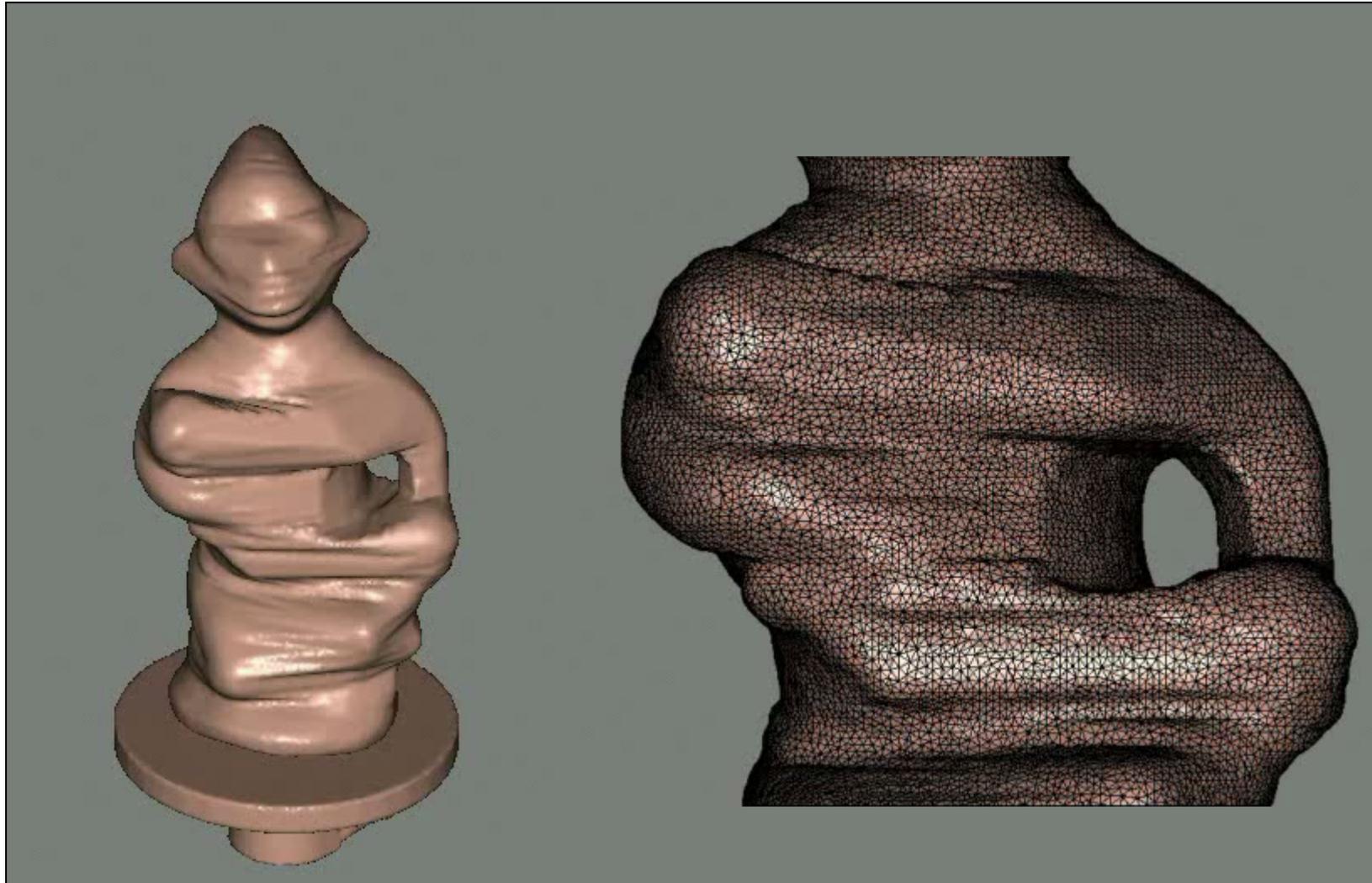


Robust NCC volume

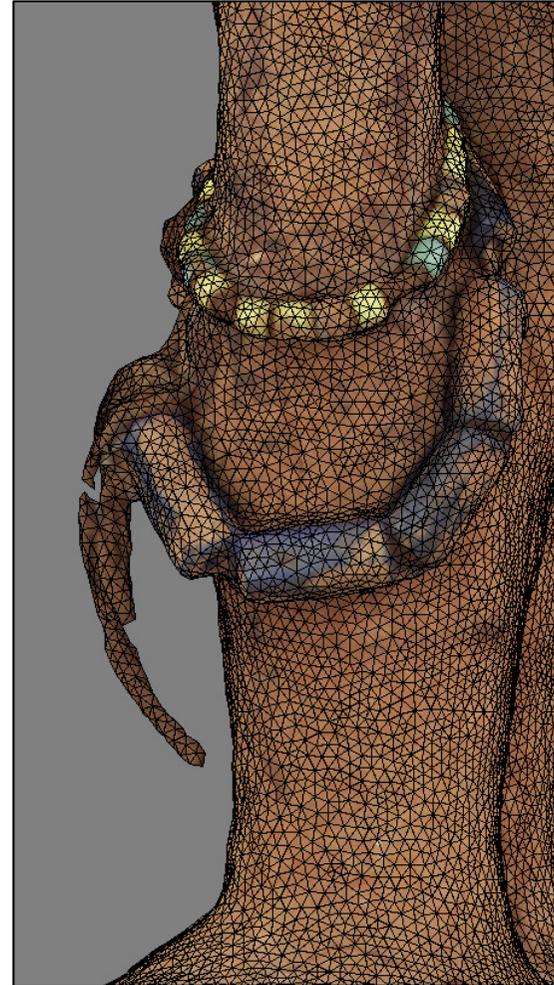
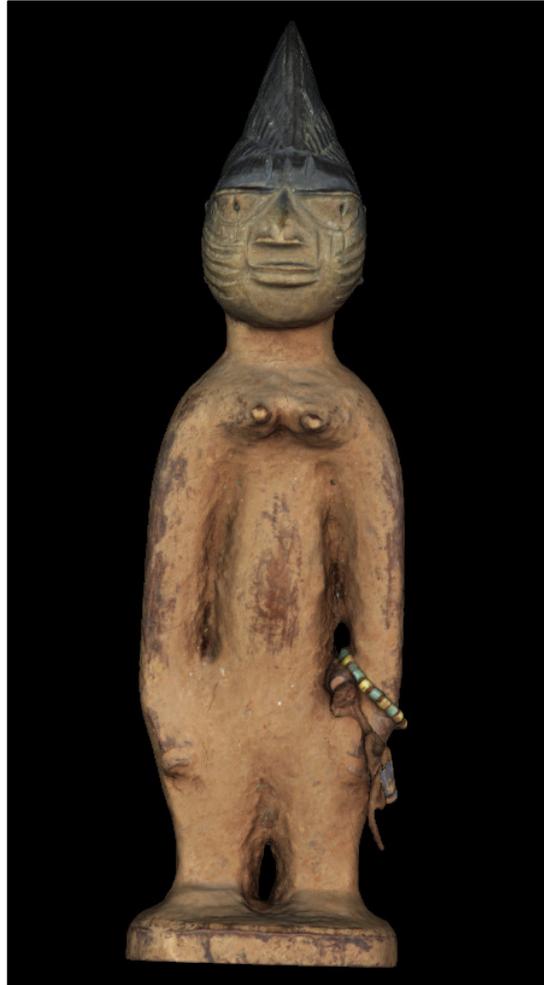


Gradient Vector Flow

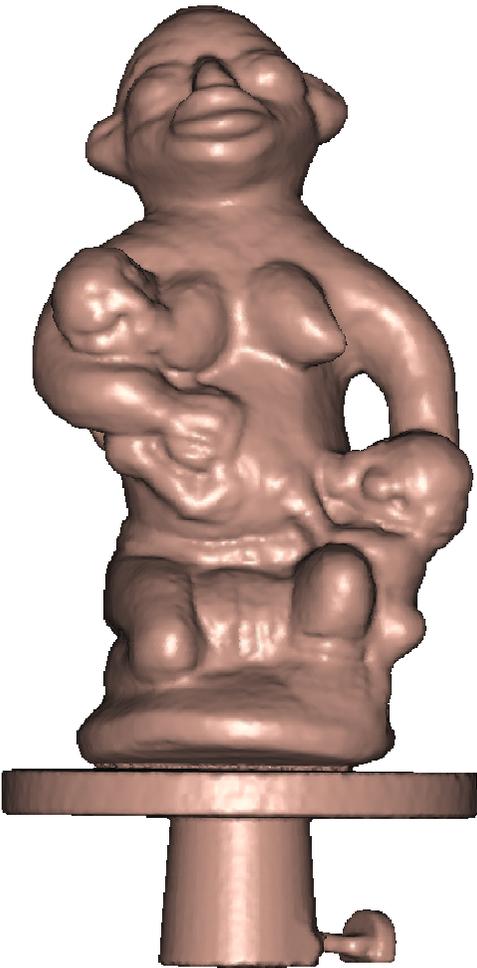
# 3D deformable meshes



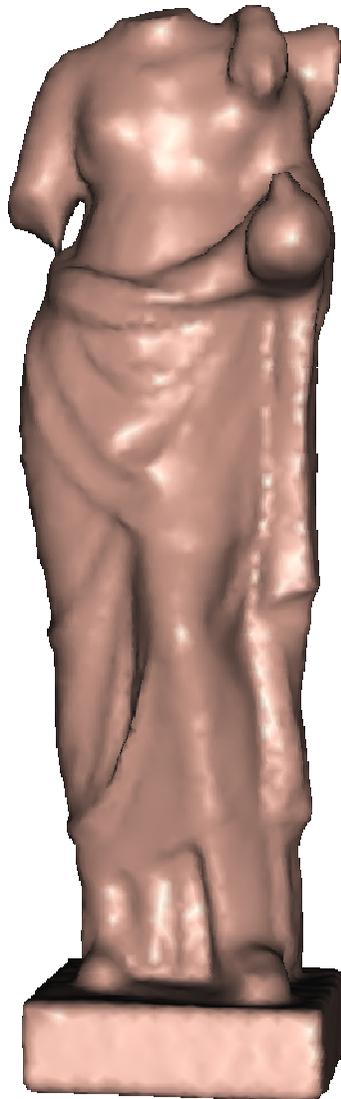
# Results



# Results



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# 3D deformable meshes

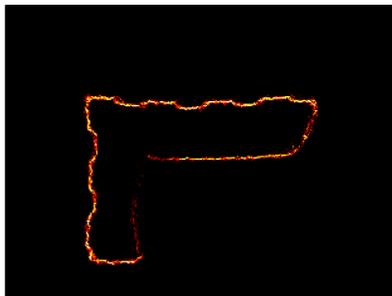
- Is local optimisation (gradient descent)
- Can get stuck in local minima
- Mesh can self-intersect
- Usually very slow
  - Typically hours of computation time
- Cannot change topology
  - That could be an advantage, more regularized
- Can we do better?

# Extracting a surface from photo-consistency

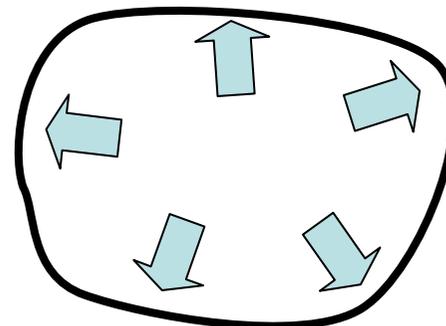
- Define a surface functional  $E[S] = \text{some cost}$
- Minimize  $E$
- Need *volume term* to avoid collapsing to a point

$$E[S] = \iint_S \rho(x) dS$$

$\rho(x) = 1.0$  - Photoconsistency



$\sigma(x) = -1$  (inflation)



# Segmentation

- In segmentation tasks we combine an edge term with a foreground/background term (e.g. 'grab-cuts' 2004)

$$E[S] = \iint_S \rho(x) dS + \iiint_{V(S)} \sigma(x) dV$$

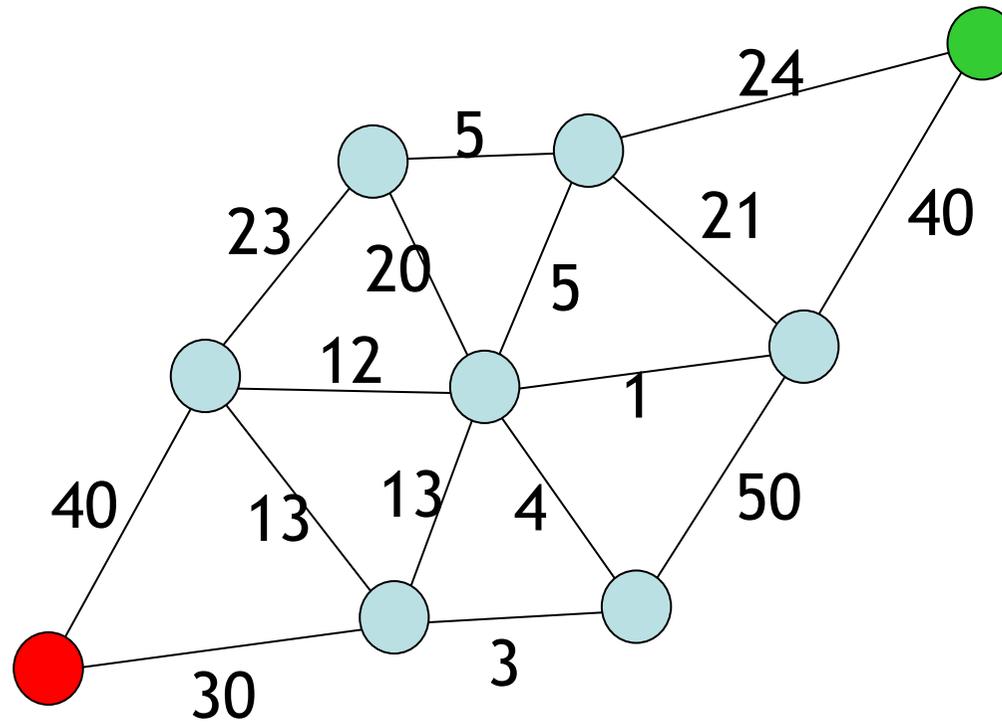
Edge cost



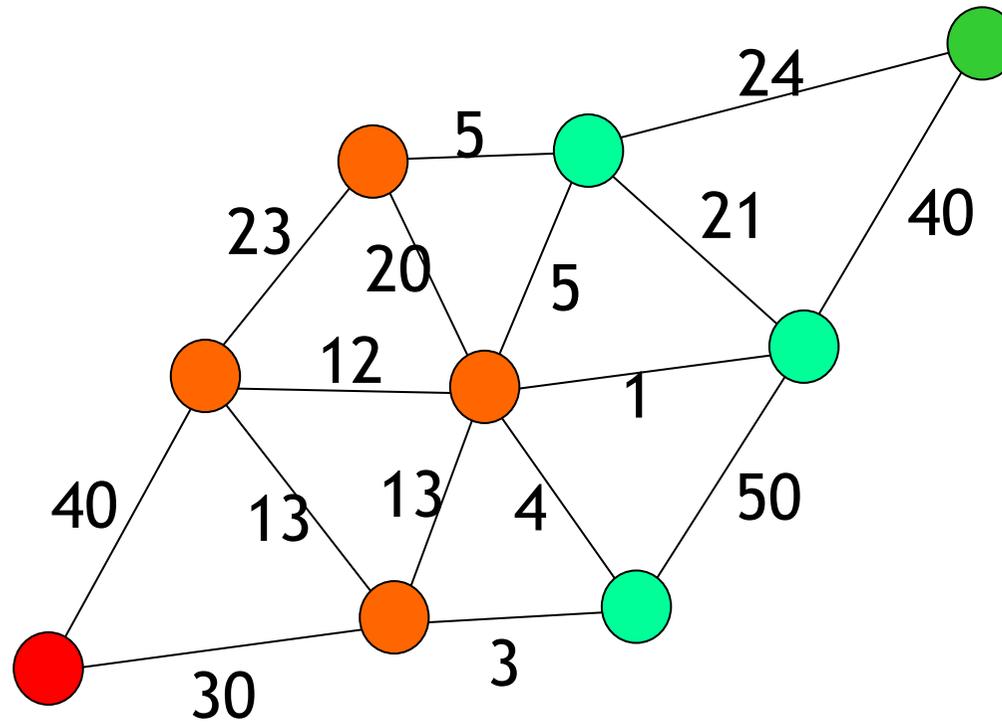
Foreground/background cost



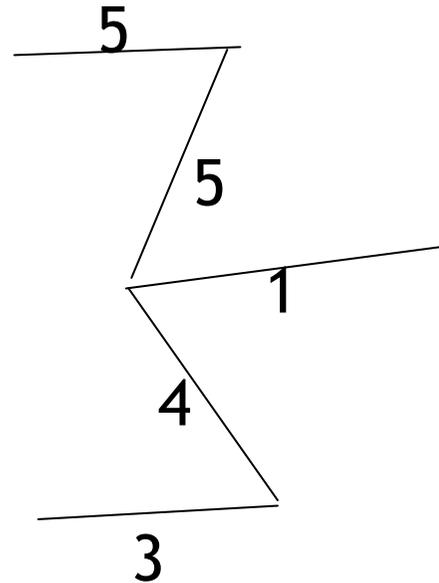
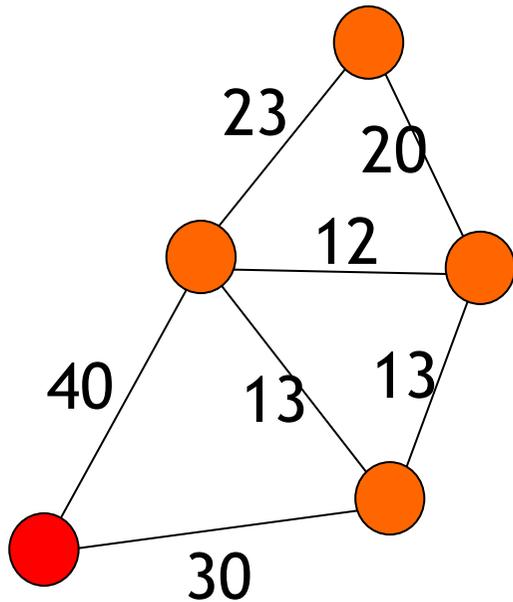
# How to solve this?



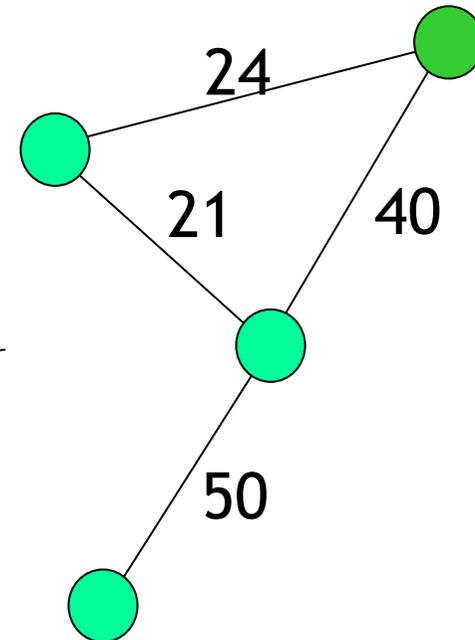
# Graph cut



# Minimum cut

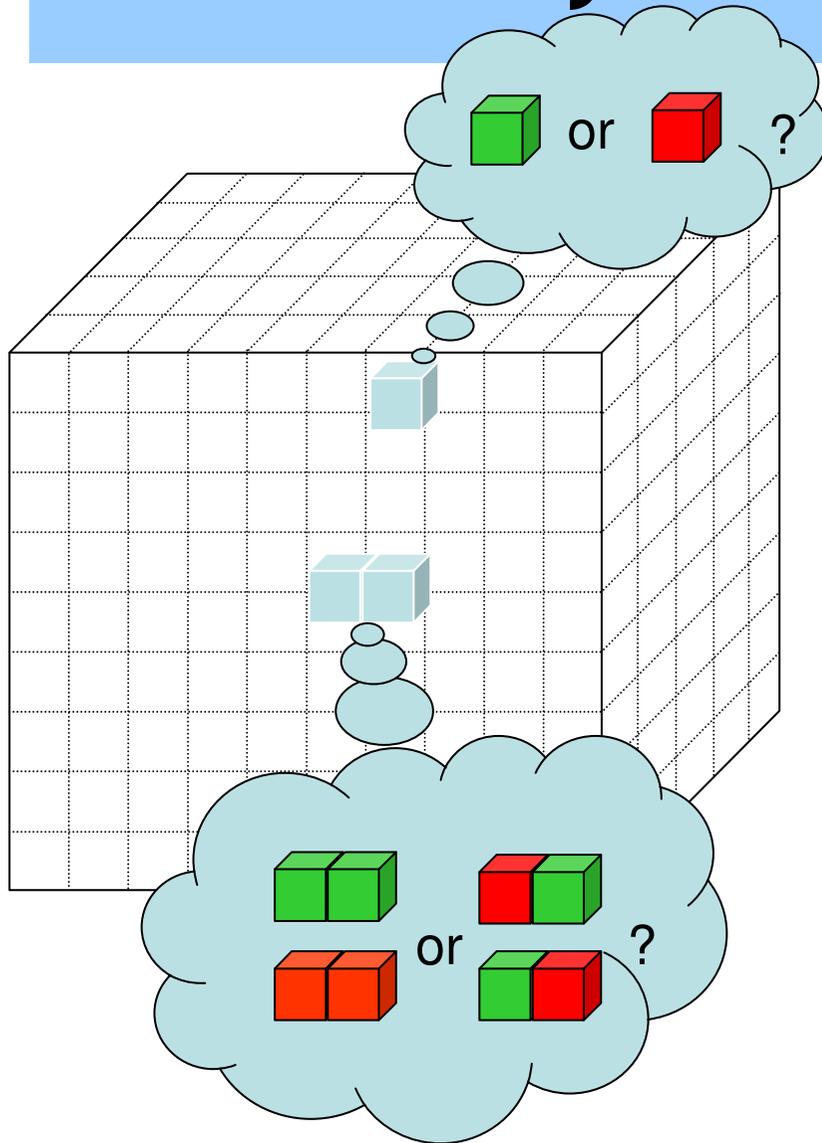


$$5+5+1+4+3=18$$



Can be computed  
in polynomial time  
with *Ford-Fulkerson* (1956)  
algorithm

# 3D binary labelling problem



Labelling cost:

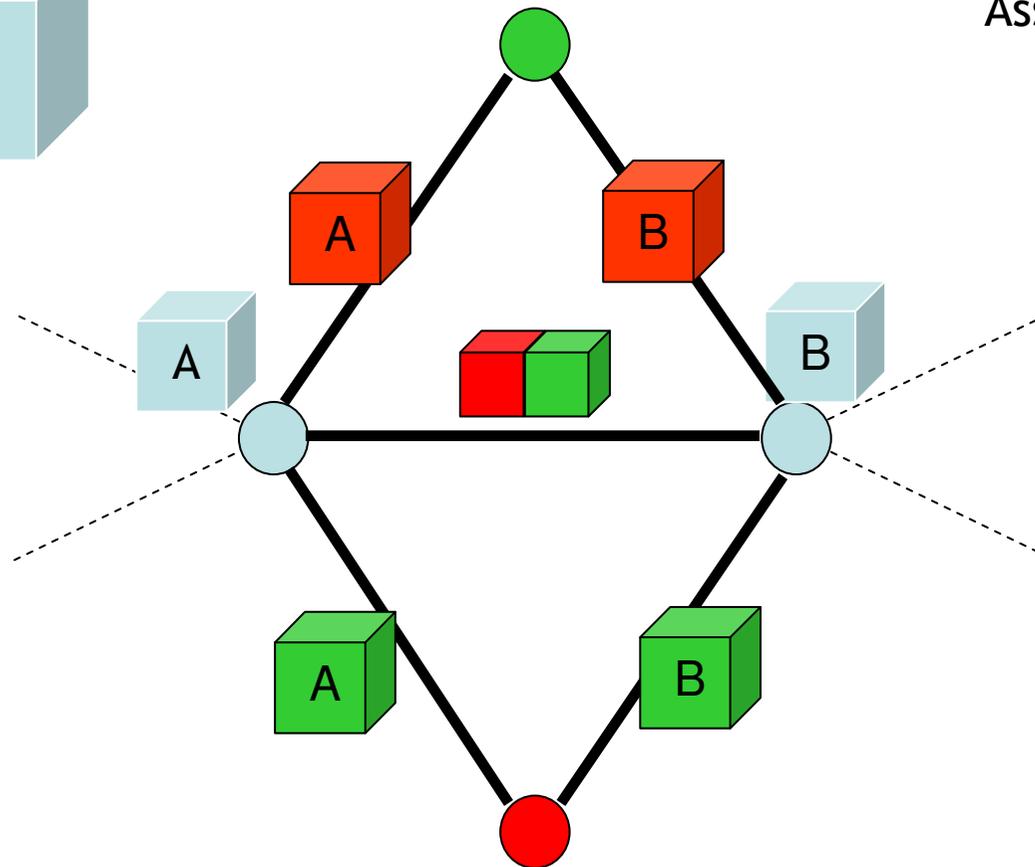
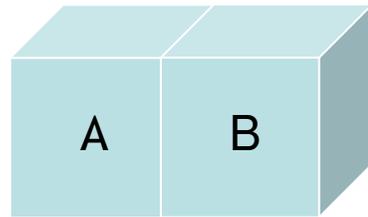
- Every voxel has a certain preference for being **foreground** or **background**

Compatibility cost:

- Every pair of neighbour voxels has a certain preference for being given the *same* or *opposite* labels
- Cost for opposite labels is greater than for same label (sub-modular)

$$\begin{array}{c} \text{Green} \text{ Green} \\ \text{Red} \text{ Red} \end{array} + \begin{array}{c} \text{Red} \text{ Red} \\ \text{Green} \text{ Green} \end{array} \leq \begin{array}{c} \text{Red} \text{ Green} \\ \text{Green} \text{ Red} \end{array} + \begin{array}{c} \text{Green} \text{ Red} \\ \text{Red} \text{ Green} \end{array}$$

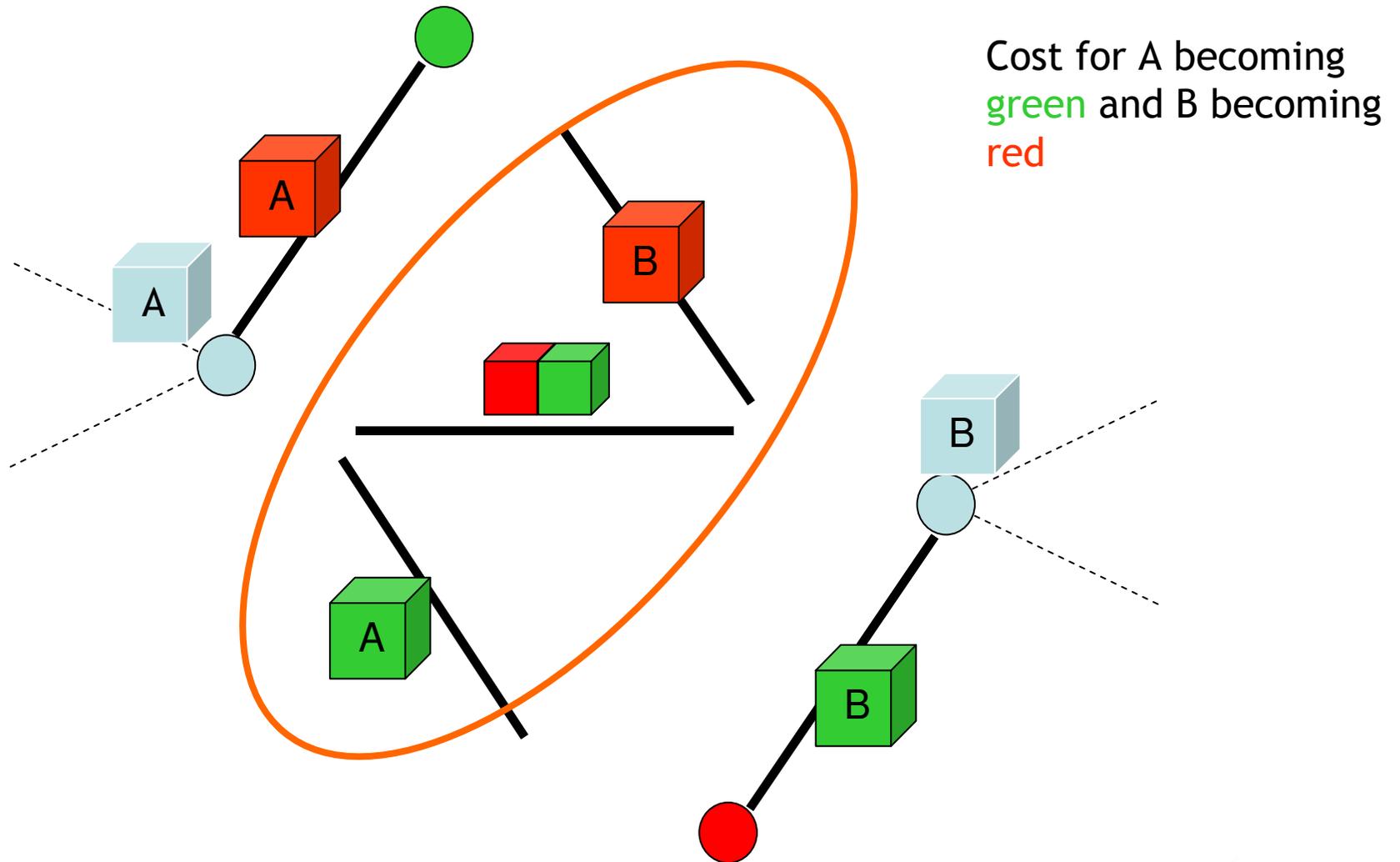
# Graph-cuts for binary MRFs



Assume

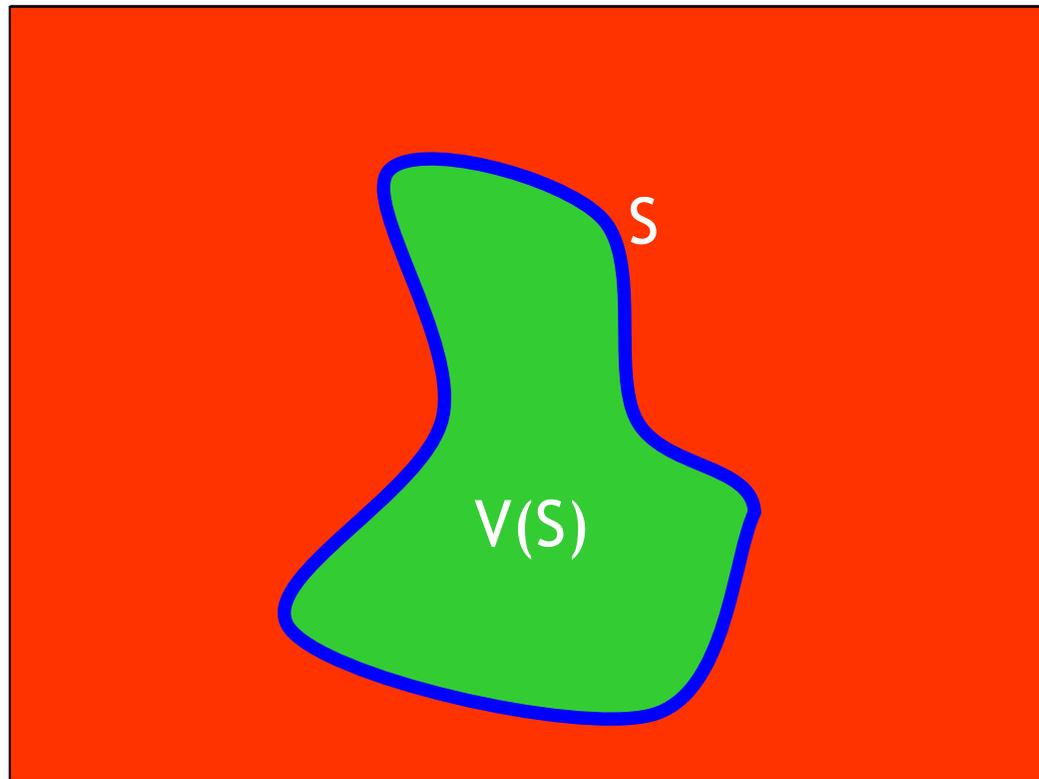
$$\begin{aligned} \text{Green} \text{ Green} &= \text{Orange} \text{ Orange} = 0 \\ \text{Red} \text{ Green} &= \text{Green} \text{ Red} \end{aligned}$$

# Graph-cuts for binary MRFs



# Binary occupancy representation

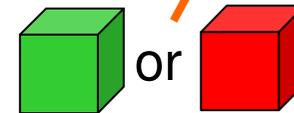
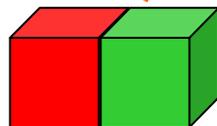
Green = IN  
Red = OUT



# Continuous functional

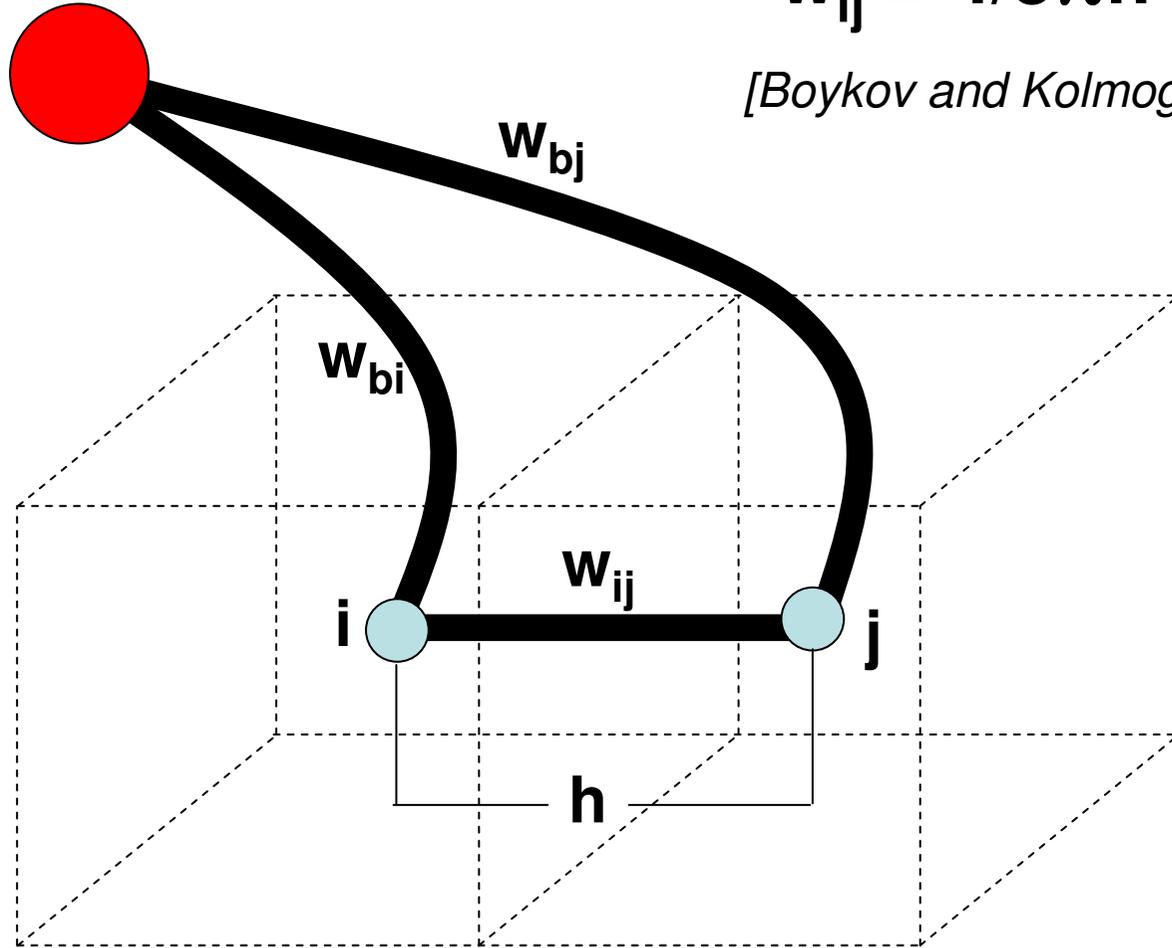
- 3D binary MRFs can be seen as discrete approximation to surface + volume integral

$$E[S] = \iint_S \rho(x) dS + \iiint_{V(S)} \sigma(x) dV$$



# Graph construction

SOURCE



$$w_{ij} = \frac{4}{3}\pi h^2 * (\rho_i + \rho_j)/2$$

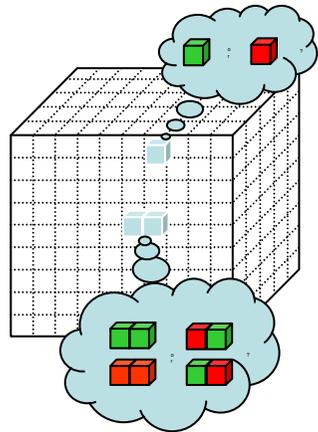
[Boykov and Kolmogorov ICCV 2001]

$$w_{bi} = \sigma_i h^3$$

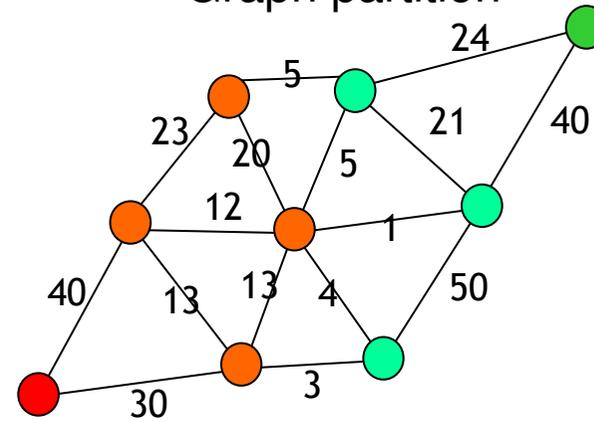
$$w_{bj} = \sigma_j h^3$$

# Three equivalent representations

Binary labelling



Graph partition

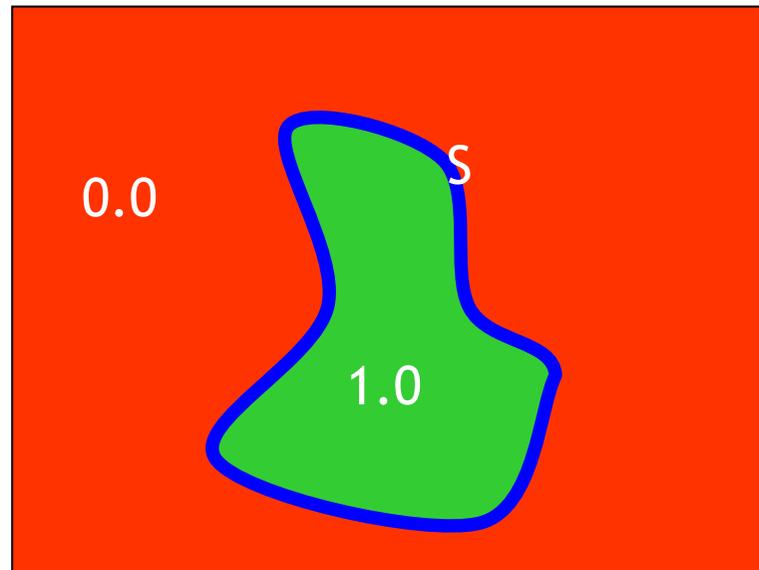


Continuous functional

$$E[S] = \iint_S \rho(x) dS + \iiint_{V(S)} \sigma(x) dV$$



# Extracting surface from binary map



- Surface can be extracted by marching cubes algorithm
- **Matlab:** `[tri, pts] = isosurface(V)`
  - $V$  is binary 3d volume of 0.0s and 1.0s
  - $pts$  is a  $3 \times N$  set of 3d points
  - $tri$  is a  $3 \times M$  set of vertex indices denoting mesh faces

# Results

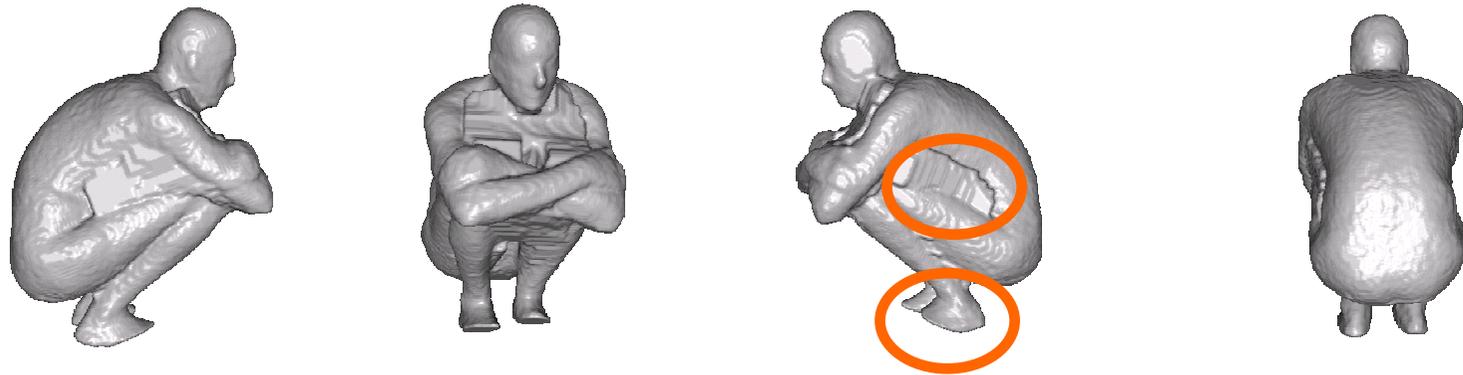


# Results



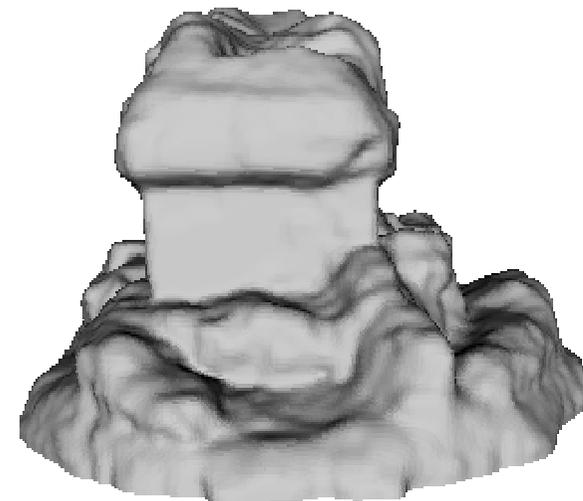
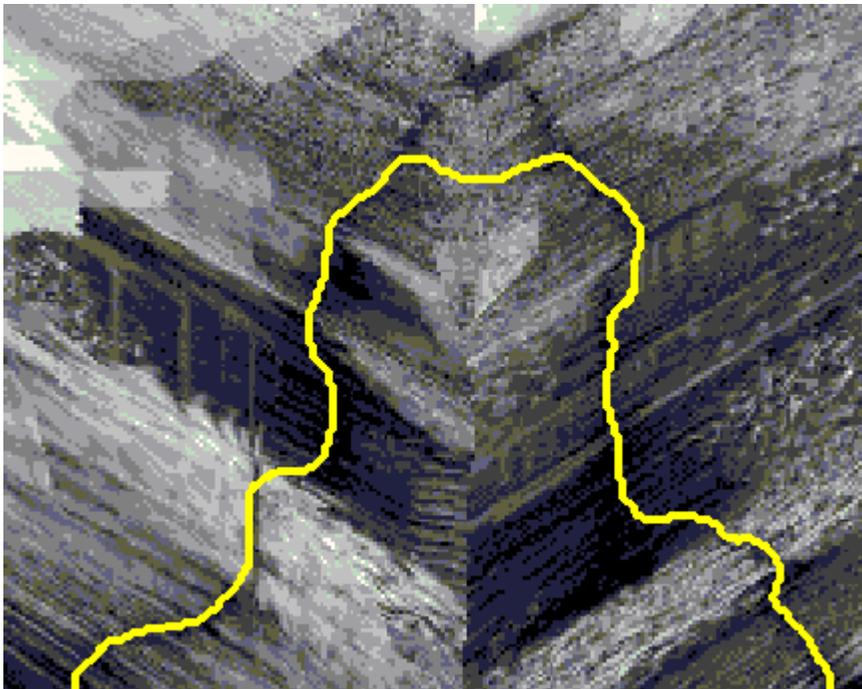
gcut3d binary

# Results

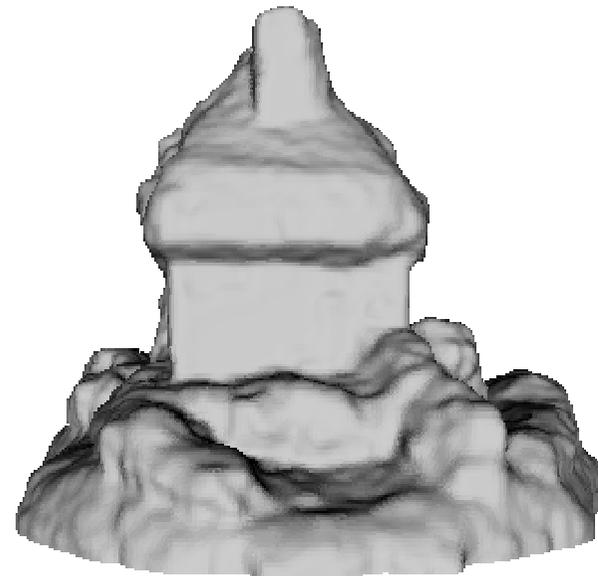
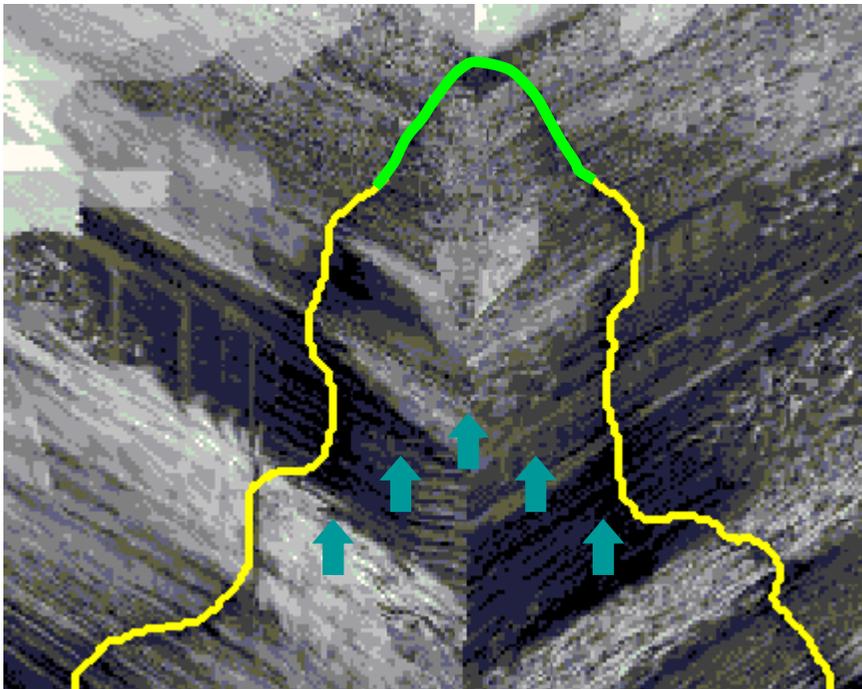


- Problem with concave regions and protrusions

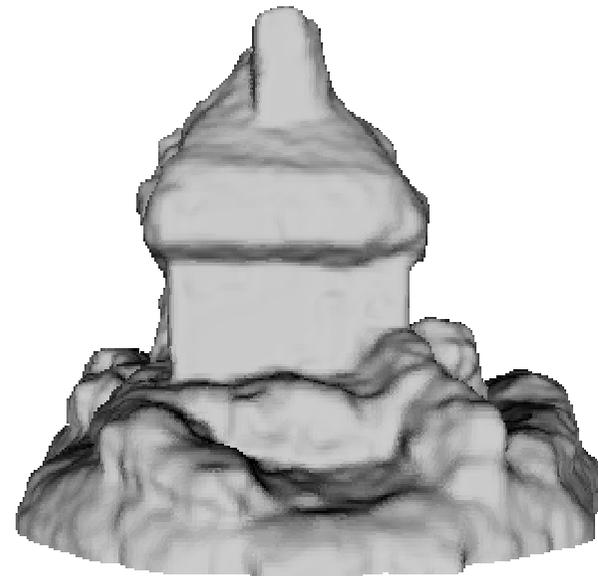
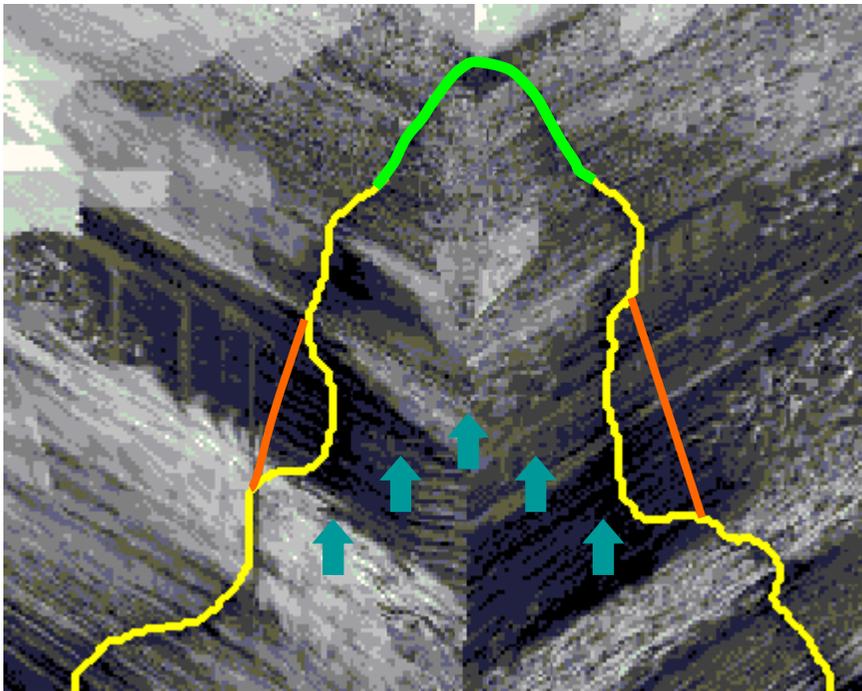
# Protrusion problem



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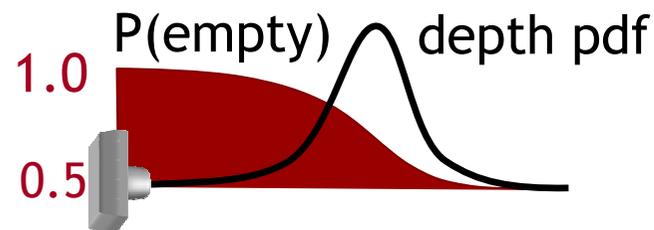
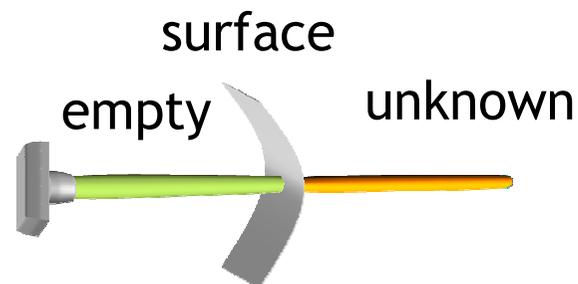


# Protrusion problem



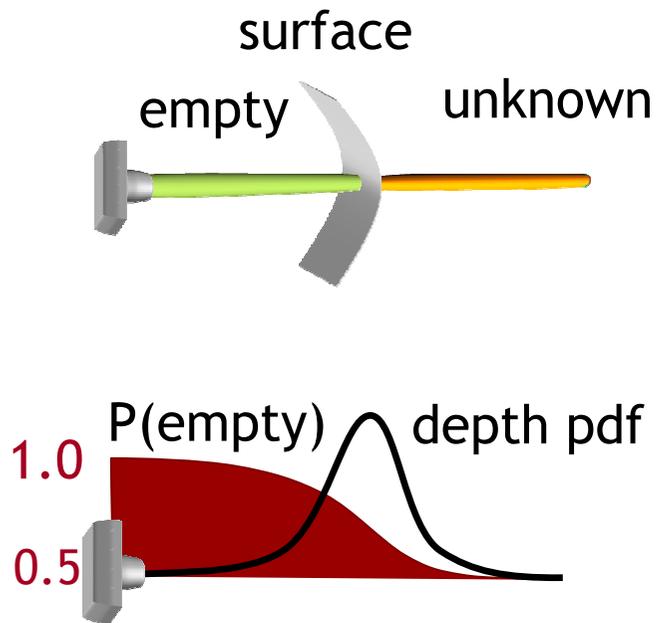
# Data driven volume term

- When a camera makes a depth measurement, also gives info about empty space

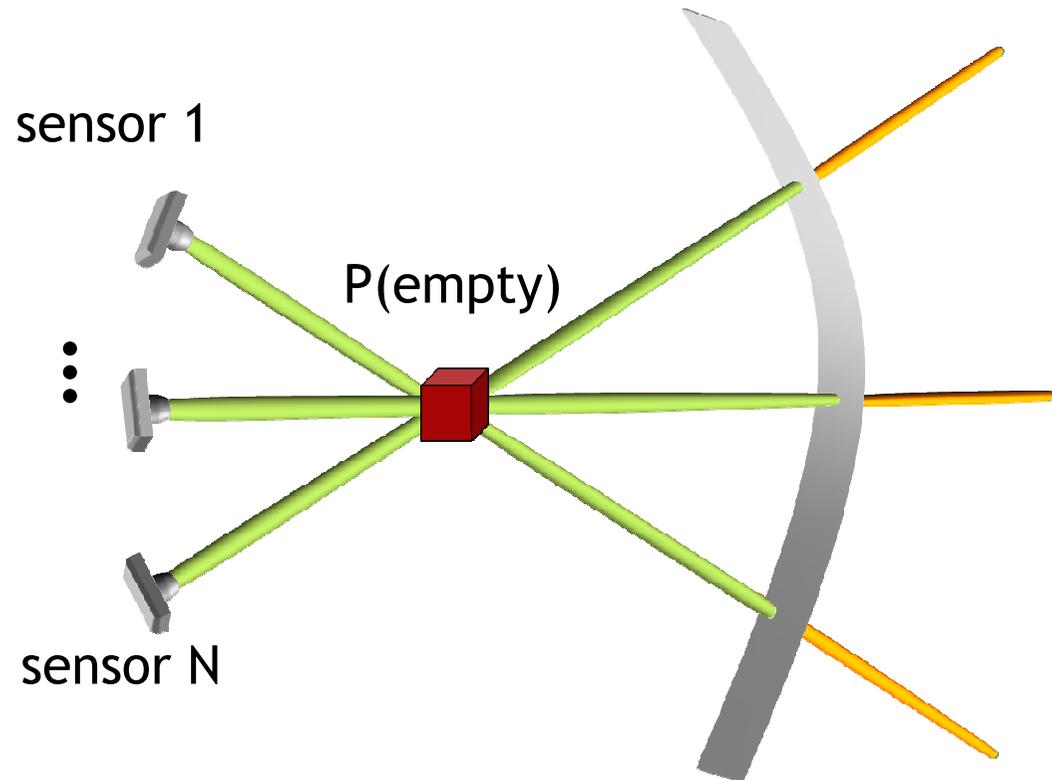


# Data driven 3D MRF labelling cost

## Probabilistic sensor model

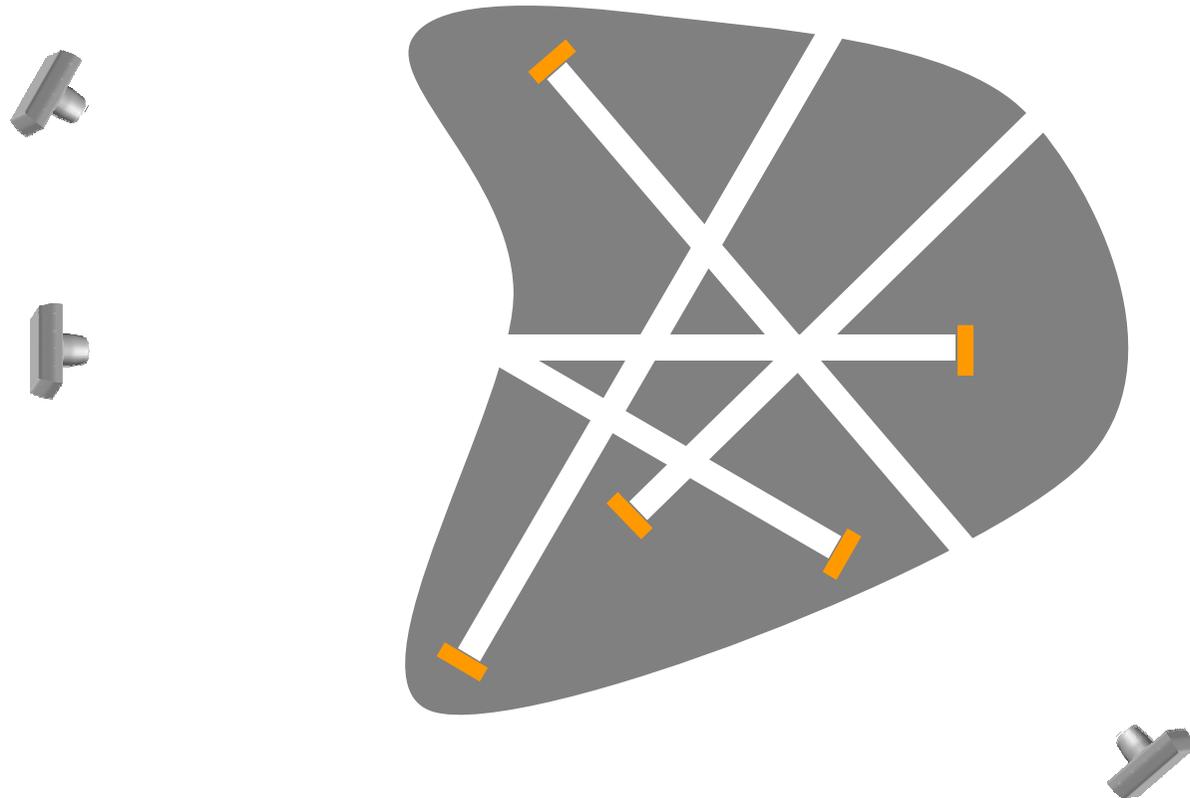


## Probabilistic sensor fusion

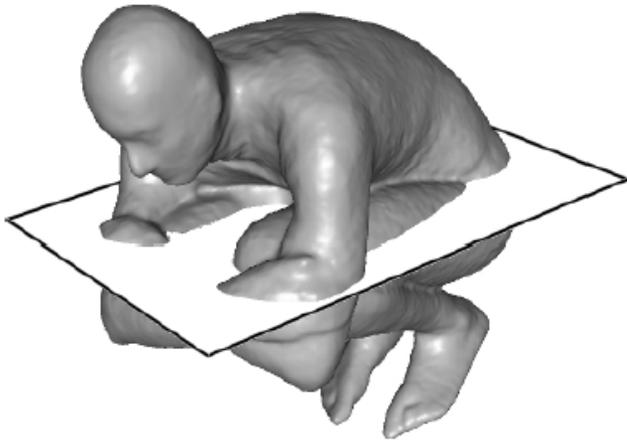


# Data driven 3D MRF labelling cost

- Problem: if sensor is too confident:



# Data driven 3D MRF labelling cost

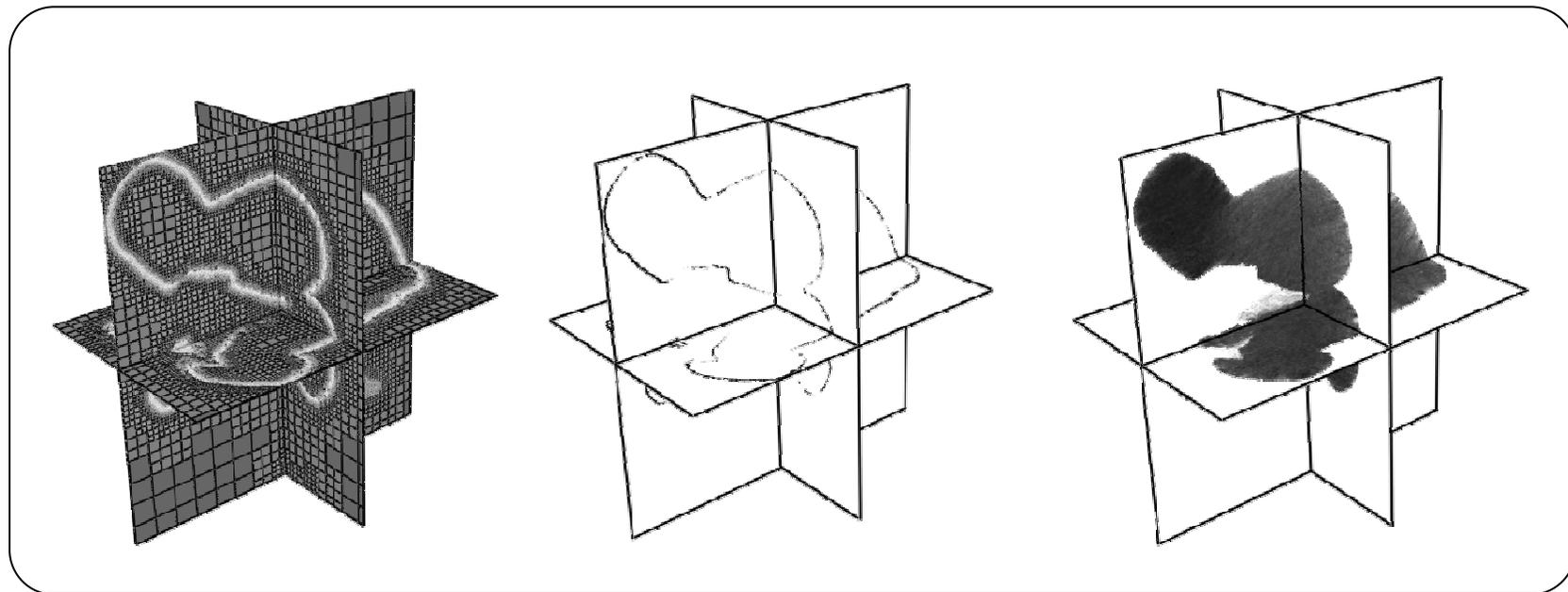


100% trusted sensor

When sensor gets depth wrong, we ‘drill hole’  
inside the volume

Solution: sensor depth distribution = Gaussian + Outlier

# 3D MRF for 3D modelling



Multi-resolution  
grid

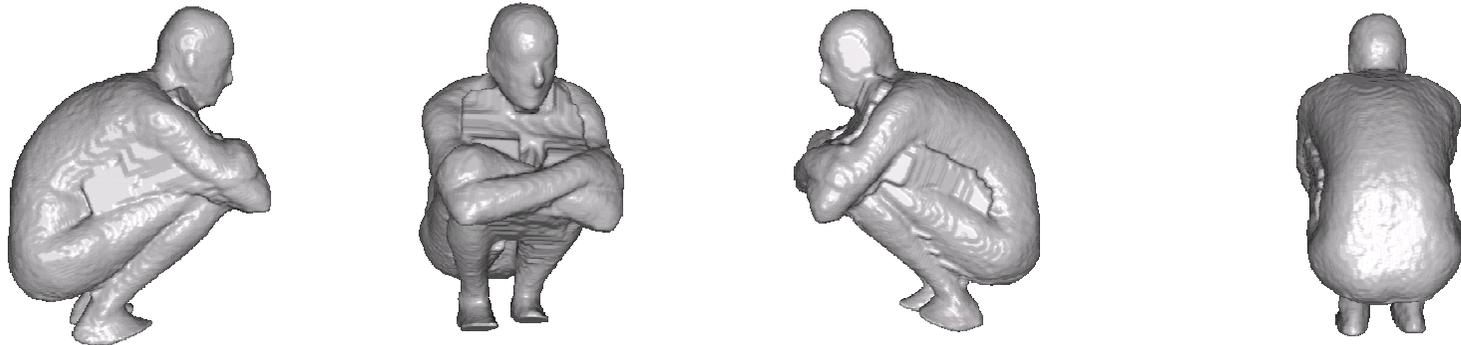
Edge  
cost

Foreground/  
background  
cost

# Results



constant  
ballooning



data-driven  
ballooning

